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## radar equation

An equation expressing the power of a radar echo at the input of the receiving antenna of a radar as a function of the range and radar cross section of a target.

For a point target and plane-polarized radiation, it is written

$$P_r = P_t \frac{G^2 \lambda^2 \sigma}{64 \pi^3 r^4},$$

where  $P_r$  is the received power,  $P_t$  the peak power transmitted by the radar,  $G$  the gain of the antenna,  $\lambda$  the wavelength,  $r$  the distance to the target, and  $\sigma$  the radar cross section of the target. For a distributed target such as precipitation, which fills the radar beam, the radar equation may be written

$$\overline{P_r} = P_t \frac{G^2 \lambda^2 \theta \phi h}{1024 \pi^2 \ln 2} \frac{\eta}{r^2},$$

where  $\theta$  and  $\phi$  denote the antenna beamwidths in the horizontal and vertical planes,  $h$  is the pulse length of the transmitted signal, and  $\eta$  is the radar reflectivity of the target. This equation assumes that the antenna pattern has a Gaussian shape and that the scattering volume is uniformly filled. The radar signals received from distributed targets fluctuate; the overbar on  $P_r$  indicates that it is a time average over a period equal to several multiples of the coherence time of the received signal. From the radar equation, the fundamental measurable property of precipitation is the radar reflectivity  $\eta$ , which depends on the sizes and concentration of the hydrometeors and their thermodynamic phase. For hydrometeors small enough for the Rayleigh scattering approximation, it is given by

$$\eta = \frac{|K|^2 \pi^5}{\lambda^4} Z,$$

where

$|K|^2$  is a dielectric factor, approximately equal to 0.93 for water and 0.21 for ice. The factor  $Z$  is called the radar reflectivity factor of the precipitation. It equals the sum of the sixth-powers of the diameters of the water drops in a unit volume of space or of the melted diameters of the snow and ice particles in a unit volume. It may be expressed in terms of the drop-size distribution as

$$Z = \int_0^\infty N(D) D^6 dD,$$

where  $N(D) dD$  is the number of drops per unit volume with diameters in the interval  $dD$ . (For ice-phase precipitation,  $N(D)$  is the distribution of melted diameters.)

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- This page was last modified on 25 April 2012, at 19:42.

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