

Antene in razširjanje valov #1

#1

1/10/2013

Fizikalne veličine:

- merske enote
- skalarji in vektorji

Skalarni produkt:

$$W[\text{J}] = \vec{F}[\text{N}] \cdot \vec{s}[\text{m}]$$

$$W = |\vec{F}| |\vec{s}| \cos \alpha$$

Vektorski produkt:

$$\vec{\omega}[\text{m/s}] = \vec{\omega}[\text{rd/s}] \times \vec{r}[\text{m}]$$

$$|\vec{\omega}| = |\vec{\omega}| |\vec{r}| \sin \alpha$$

smerni \vec{v} ?

Koordinatni sistemi:

1) 3D

2) PRAVOKOTNI $\vec{e}_x \cdot \vec{e}_y = 0$

3) DESNOROČNI $\vec{e}_x \times \vec{e}_y = \vec{e}_z$

Kartezijski KS (x, y, z):

$$\vec{r} = x\vec{e}_x + y\vec{e}_y + z\vec{e}_z$$

$$|\vec{r}| = \sqrt{x^2 + y^2 + z^2}$$

$$\vec{r} \cdot \vec{s} = x_1x_2 + y_1y_2 + z_1z_2$$

$$\vec{r} \times \vec{s} = \begin{vmatrix} \vec{e}_x & \vec{e}_y & \vec{e}_z \\ x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \end{vmatrix}$$

Krogelni KS (r, θ, φ):

$$0 \leq r[\text{m}] < \infty$$

$$0 \leq \theta[\text{rad}] \leq \pi$$

$$0 \leq \phi[\text{rad}] < 2\pi$$

$$x = r \sin \theta \cos \phi$$

$$y = r \sin \theta \sin \phi$$

$$z = r \cos \theta$$

$$\textcircled{1} \quad l_1 = h_\theta \Delta \theta; \quad h_\theta = r = 111 \text{ km/}^\circ$$

$$\textcircled{2} \quad l_2 = h_\phi \Delta \phi; \quad h_\phi = r \sin \theta = 111 \text{ km/}^\circ \cdot \sin \theta$$

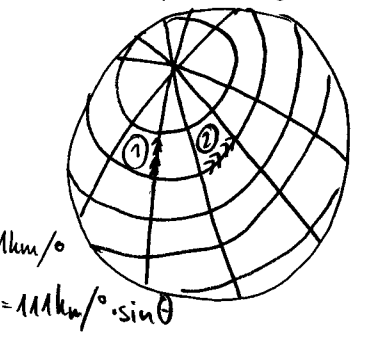
Krivočrtni KS (q₁, q₂, q₃):

$$dl_i = h_i dq_i$$

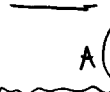
$$h_i = \sqrt{\left(\frac{\partial x}{\partial q_i}\right)^2 + \left(\frac{\partial y}{\partial q_i}\right)^2 + \left(\frac{\partial z}{\partial q_i}\right)^2}$$

$$\text{Zemljepis:}$$

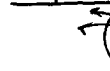
$$\lambda = \phi, \quad \varphi = \theta - \theta_0$$



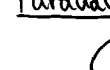
Gauss:



Ampere:



Faraday:



ME:

$$\textcircled{1} \quad \text{rot } \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$\textcircled{2} \quad \text{rot } \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\textcircled{3} \quad \text{div } \vec{D} = \rho$$

$$\frac{\partial \vec{D}}{\partial t} = \vec{J}_D$$

$$\vec{J} = \sigma \vec{E}$$

$$\vec{B} = \mu \vec{H}$$

$$\vec{E} = -\frac{\partial \vec{A}}{\partial t} - \text{grad } V$$

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Ponovitev: sevanje masega dipola $l \ll \lambda$

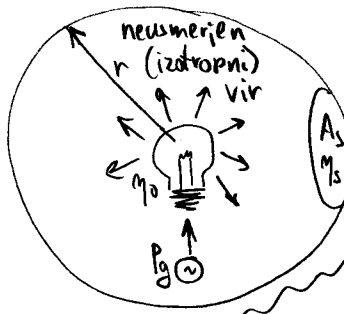
$$\vec{E} = \vec{I}_0 \frac{j k z_0}{4\pi} I l \frac{e^{jkr}}{r} \sin\theta$$

$$\vec{H} = \vec{I}_0 \frac{j k}{4\pi} I l \frac{e^{jkr}}{r} \sin\theta$$

$$\vec{S} = \frac{1}{2} \vec{E} \times \vec{H}^* = \vec{I}_r \frac{k^2 z_0 I l^2}{32\pi^2} \frac{\sin^2\theta}{r^2}$$

$$P_s = \oint_A \vec{S} \cdot \vec{n} dA = \frac{k^2 z_0 I l^2}{12\pi} = \frac{1}{2} I l^2 R_s$$

$$R_s = \frac{k^2 z_0 l^2}{6\pi} = \frac{2\pi z_0}{3} \left(\frac{l}{\lambda}\right)^2$$



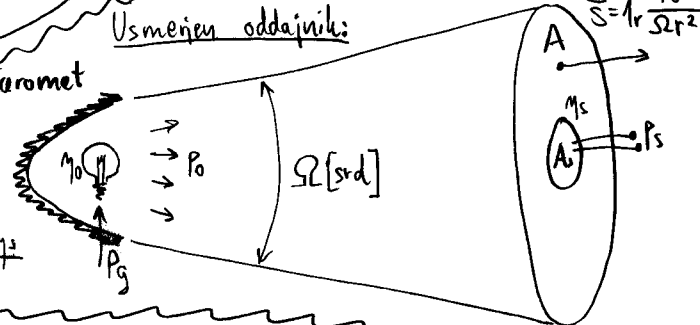
$$\vec{S} = \vec{I}_r \frac{P_0}{4\pi r^2} = \frac{P_g \mu_0}{4\pi r^2}$$

$$\Omega = 4\pi$$

$$A = 4\pi r^2$$

$$P_s = m_s \int_{A_s} \vec{S} \cdot \vec{n} dA = |\vec{S}| A_s m_s = \frac{P_g \mu_0 A_s m_s}{4\pi r^2}$$

Usmerjen oddajnik:



Smernost
(Directivity)

$$D = \frac{|\vec{S}|}{|\vec{S}|_{\text{avg}}} = \frac{4\pi}{\Omega} \geq 1 \quad P_s = \frac{P_g D \mu_0 A_s m_s}{4\pi r^2}$$

Poljubni oddajnik:

$$\vec{E} = \vec{I}_p \propto I \frac{e^{jkr}}{r} F(\theta, \phi)$$

↑
POLARIZACIJA VIR

↑
SEVANJE

↑
ANTENNI
SMERNI
DIAGRAM

$$\vec{S} = \frac{1}{2} \vec{E} \times \vec{H}^* = \vec{I}_r \frac{|\vec{E}|^2}{2z_0}$$

$$D = \frac{|\vec{S}|}{|\vec{S}|_{\text{avg}}} = \frac{4\pi r^2 \frac{|\vec{E}|^2}{2z_0}}{\int_{4\pi} \frac{|\vec{E}|^2}{2z_0} r^2 d\Omega} = \frac{4\pi |F(\theta_{\text{max}}, \phi_{\text{max}})|^2}{\int_{4\pi} |F(\theta, \phi)|^2 \sin\theta d\theta d\phi}$$

Zgled:

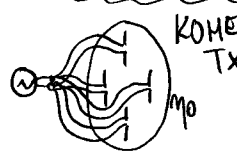
$$F(\theta, \phi) = \sin\theta$$

$$D = 1.5$$

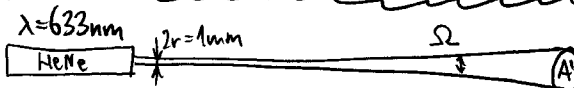
Dobitek (Gain):

$$G = \eta D$$

Log. enote: $G [\text{dBi}] = 10 \log_{10} G [\text{lin}]$, $D [\text{dBi}] = 10 \log_{10} D [\text{lin}]$



$$D = \frac{4\pi}{\Omega} A$$



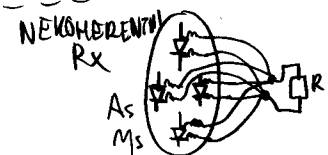
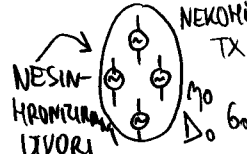
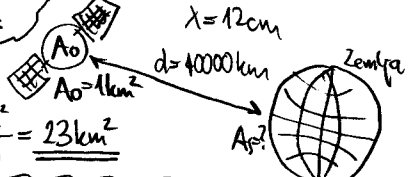
$$D = \frac{4\pi}{\Omega} A = 2.5 \cdot 10^7 = 74 \text{ dBi}$$

$$\Omega = \frac{4\pi}{D} = 5 \cdot 10^{-7} \text{ srd}$$

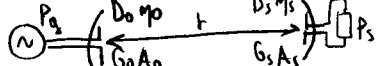
$$A' (1 \text{ km}) = 0.5 \text{ m}^2$$

Veselite se elektrarnar:

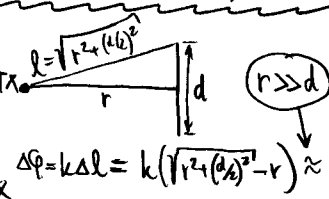
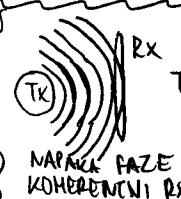
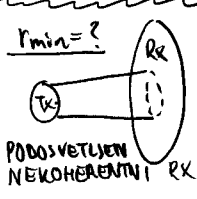
$$A_s = \Omega d^2 = \frac{4\pi}{D} d^2 = \frac{\lambda^2 d^2}{A_0} = 23 \text{ km}^2$$



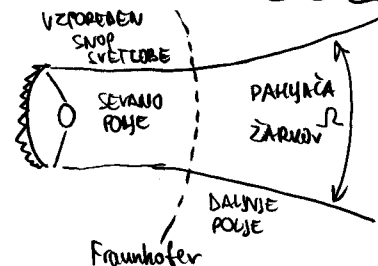
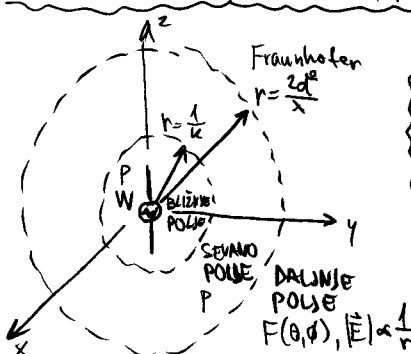
Radialna koherentna zveza:



- ① $P_s = P_g D_0 m_0 \frac{A_s m_s}{4\pi r^2} = P_g G_0 \frac{A_s m_s}{4\pi r^2} \rightarrow \text{RADIOIFUZIJA} \sim \text{NEODVISNO OD } \lambda$
- ② $P_s = P_g D_0 m_0 D_s m_s \left(\frac{\lambda}{4\pi r}\right)^2 = P_g G_0 G_s \left(\frac{\lambda}{4\pi r}\right)^2 \rightarrow \text{ZGODOVINA, TELEFON, } \lambda^2$
- ③ $P_s = P_g \frac{A_0 m_0 A_s m_s}{r^2 \lambda^2} \rightarrow \text{CILJANJE?} \rightarrow \text{TOČKA-TOČKA} \sim \lambda^{-2}$



$r_{\text{min}} = \frac{k d^2}{8\Delta\phi}$	$\Delta\phi$	ΔG	r_{min}	cc
$r_{\text{min}} = \frac{\pi d^2}{4\Delta\phi}$	$\pi/2$	-4dB	$d^2/4\lambda$	$\rightarrow \text{globuska ostrina}$
	$\pi/4$	-1dB	$d^2/2\lambda$	$\lambda = 0.5 \mu\text{m}, d = 1 \text{ mm} \rightarrow r_{\text{min}} = 0.5 \text{ m}$
	$\pi/8$	-0.25dB	d^2/λ	$\rightarrow \text{točne! Fraunhofer}$
		-0.06dB	$2d^2/\lambda$	$\rightarrow \text{meritve anten}$



Definicija d:

PREČNO NASMER SEVANJA

ANTENA

GLAVNI SNOPI

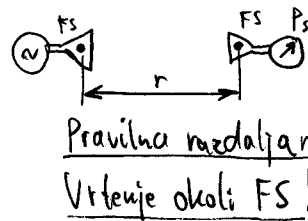
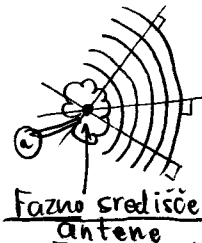
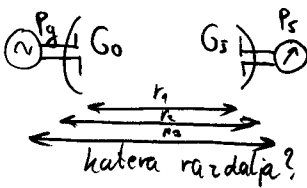
STRANSKI SNOPI

GLAVNI SNOPI

Ponovitev

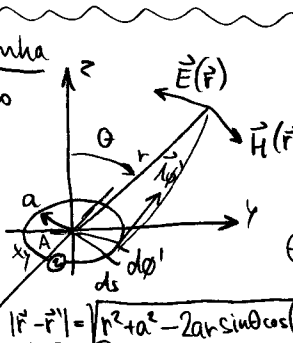
KOM. ZVEZA: $P_s = P_g G_o G_s \left(\frac{\lambda}{4\pi r}\right)^2$

Fraunhofer: $r > r_{min} = \frac{2d^2}{\lambda}$
(antene fokusirane v ∞)



Majhna zanka

- 1) $a \ll r$
- 2) $a \ll \lambda$



$$\vec{A} = \frac{\mu_0}{4\pi} \int_0^{2\pi} \vec{I} \frac{e^{-jk|\vec{r}-\vec{r}'|}}{|\vec{r}-\vec{r}'|} a d\phi'$$

$$\frac{1}{|\vec{r}-\vec{r}'|} \approx \frac{1}{r} \left(1 + \frac{a}{r} \sin\theta \cos(\theta-\phi')\right)$$

$$e^{-jk|\vec{r}-\vec{r}'|} \approx e^{-jkr} (1 + jk a \sin\theta \cos(\theta-\phi'))$$

$$\vec{r}' = -\vec{r}_x \sin\phi' + \vec{r}_y \cos\phi'$$

$F(\theta, \phi) = A(\theta, \phi) e^{j\phi(\theta, \phi)}$
Re konst!

Nekatere antene nimajo FS?

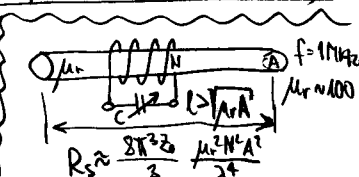
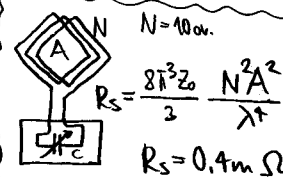
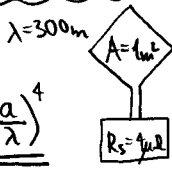
$\vec{A} \approx \vec{r}_\phi \frac{\mu_0}{4\pi} I \pi a^2 \frac{e^{jkr}}{r} (jk + \frac{1}{r}) \sin\theta$ $A = \pi a^2$

$\vec{E} = -j\omega \vec{A} - \text{grad} V \approx \vec{r}_\phi \frac{k^2 Z_0}{4\pi} I A \frac{e^{jkr}}{r} \sin\theta$

$\vec{H} = \frac{1}{\mu_0} \text{rot} \vec{A} = \left(\text{skalarni } \frac{1}{r}, \frac{1}{r}, \frac{1}{r}\right)$

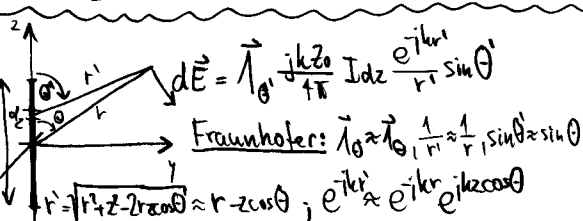
$\vec{S} = \vec{r} \frac{|\vec{E}|^2}{2Z_0} = \vec{r} \frac{k^4 Z_0}{32\pi^2} |I|^2 A^2 \frac{\sin^2\theta}{r^2}$

$R_s = \frac{P}{\frac{1}{2}|I|^2} = \frac{k^4 Z_0}{6\pi} A^2 = \frac{8\pi^3 Z_0}{3} \frac{A^2}{\lambda^4} = \frac{8\pi^3 Z_0}{3} \left(\frac{a}{\lambda}\right)^4$



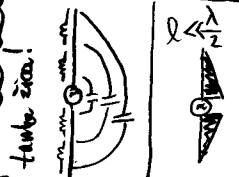
Dolga zanka

$l \sim \lambda$



Fraunhofer: $\vec{r}_0 \approx \vec{r}_1, \frac{1}{r} \approx \frac{1}{r}, \sin\theta \approx \sin\theta$
 $\vec{r} = \sqrt{r^2 + z^2 - 2rz\cos\theta} \approx r - z\cos\theta, e^{jkr} \approx e^{jkr} e^{jkz\cos\theta}$

Porezdelitev toka?



$l = \frac{\lambda}{2}$

$l = \lambda$

$l = \frac{3\lambda}{2}$

$l = \frac{5\lambda}{2}$

Polvalovni dipol:

$I(z) = I_0 \cos kz$

$\vec{E} = \int_{-\frac{\lambda}{4}}^{\frac{\lambda}{4}} d\vec{E} = \vec{r}_\theta \frac{j k Z_0}{4\pi} \frac{e^{jkr}}{r} \sin\theta \int_{-\frac{\lambda}{4}}^{\frac{\lambda}{4}} \cos kz e^{jkz\cos\theta} dz$

$dz = \vec{r}_\theta \frac{j Z_0}{2\pi} I_0 \frac{e^{jkr}}{r} \frac{\cos(\frac{\pi}{2}\cos\theta)}{\sin\theta} F(\theta, \phi) = \frac{\cos(\frac{\pi}{2}\cos\theta)}{\sin\theta}$

$\vec{S} = \vec{r} \frac{Z_0}{8\pi^2} |I_0|^2 \frac{\cos^4(\frac{\pi}{2}\cos\theta)}{r^2 \sin^2\theta}$

$R_s = \frac{1}{2|I_0|^2} \int \vec{S} \cdot \vec{r} r^2 \sin\theta d\theta d\phi = \frac{Z_0}{2\pi} I = 60\Omega I = 73\Omega$

$I = \int_{-1}^{+1} \frac{\cos^2(\frac{\pi}{2}u)}{1-u^2} du = 1.22$

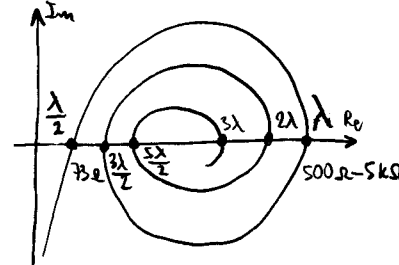
Smernost:

$D = \frac{4\pi |F(\theta_m, \phi_m)|^2}{\int |F(\theta, \phi)|^2 d\Omega} = \frac{4\pi}{2\pi \int_0^\pi \frac{\cos^2(\frac{\pi}{2}\cos\theta)}{\sin^2\theta} \sin\theta d\theta} = \frac{2}{I} = 1.64 = 2.15 \text{ dBi}$

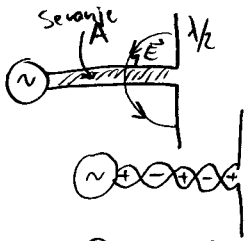
Primerjava s polvalovnim dipolom

$D[\text{dBi}] = 10 \log_{10} D = D[\text{dBd}] + 2.15 \text{ dB}$

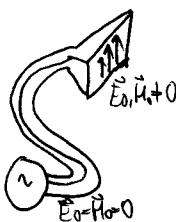
Impedanca dipole $Z(l)$:



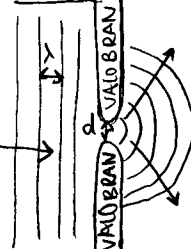
PONOVITEV: NAPAJANJE DIPOLA



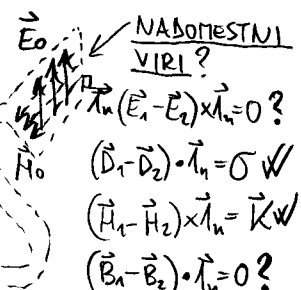
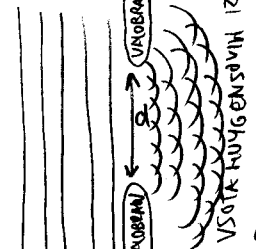
LJAK IN VALOVOD



HUYGENSOV

IZVOR: $d \ll \lambda$ 

HUYGENS-OVO

NAČELO: $d \ll \lambda$ 

Razširjene ME:

① $\text{rot } \vec{H} = \vec{J} + j\omega \vec{E}$

② $\text{rot } \vec{E} = -\vec{J}_m - j\omega \vec{H}$

③ $\text{div}(\epsilon \vec{E}) = \rho$

④ $\text{div}(\mu \vec{H}) = \rho_m$

Razširjeni preslopi

pogoji:

$(\vec{E}_1 - \vec{E}_2) \times \vec{n} = -\vec{K}_m$

$(\vec{D}_1 - \vec{D}_2) \cdot \vec{n} = \sigma$

$(\vec{H}_1 - \vec{H}_2) \times \vec{n} = \vec{K}$

$(\vec{B}_1 - \vec{B}_2) \cdot \vec{n} = \sigma_m$

Recipročnost Lorentze:

$\text{rot } \vec{H}_1 = \vec{J}_1 + j\omega \epsilon \vec{E}_1 / \epsilon_0$

$\text{rot } \vec{E}_1 = -\vec{J}_m - j\omega \mu \vec{H}_1 / \mu_0$

$\epsilon \equiv \text{skalar} \rightarrow \vec{E}_2 \cdot \text{rot } \vec{H}_1 - \vec{E}_1 \cdot \text{rot } \vec{H}_2 = \epsilon_0 (\vec{J}_1 \cdot \vec{E}_2 - \vec{E}_1 \cdot \vec{J}_2)$

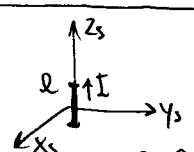
$\mu \equiv \text{skalar} \rightarrow \vec{H}_2 \cdot \text{rot } \vec{E}_1 - \vec{H}_1 \cdot \text{rot } \vec{E}_2 = -\mu_0 (\vec{J}_m1 \cdot \vec{H}_2 + \vec{H}_1 \cdot \vec{J}_m2)$

člena v enaki!

$$\int_V (\vec{E}_2 \cdot \text{rot } \vec{H}_1 - \vec{H}_1 \cdot \text{rot } \vec{E}_2 + \vec{H}_2 \cdot \text{rot } \vec{E}_1 - \vec{E}_1 \cdot \text{rot } \vec{H}_2) dV = \int_V \text{div}(\vec{H}_1 \times \vec{E}_2 + \vec{E}_1 \times \vec{H}_2) dV = \oint_{A \rightarrow \infty} (\vec{E}_1 \times \vec{H}_2 - \vec{E}_2 \times \vec{H}_1) \cdot \vec{n} dA = 0$$

$$0 = \int_V (\vec{E}_2 \cdot \vec{J}_1 - \vec{E}_1 \cdot \vec{J}_2 - \vec{H}_2 \cdot \vec{J}_m1 + \vec{H}_1 \cdot \vec{J}_m2) dV \rightarrow \int_{V_1} (\vec{E}_2 \cdot \vec{J}_1 - \vec{H}_2 \cdot \vec{J}_m1) dV_1 = \int_{V_2} (\vec{E}_1 \cdot \vec{J}_2 - \vec{H}_1 \cdot \vec{J}_m2) dV_2$$

Sonda = tokovni element:



$$\vec{E}_s = \vec{a}_\theta \frac{jk\omega \mu_0 I l}{4\pi} \frac{e^{-jkr}}{r} \sin\theta$$

$$\vec{H}_s = \vec{a}_\phi \frac{jk}{4\pi} I l_s \frac{e^{-jkr}}{r} \sin\theta$$

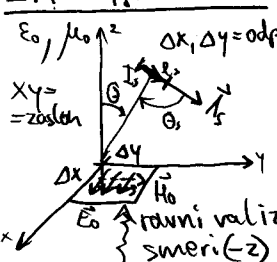
$$\vec{J}_2 = \vec{a}_s \frac{I_s}{A_s}$$

$$\vec{J}_m2 = 0$$

$$\int_{V_s} (\vec{E} \cdot \vec{J}_s - \vec{H} \cdot \vec{J}_m) dV_s = \vec{E} \cdot \vec{a}_s I_s l_s$$

$$\vec{E} \cdot \vec{a}_s = \frac{1}{I_s l_s} \int_V (\vec{E}_s \cdot \vec{J} - \vec{H}_s \cdot \vec{J}_m) dV$$

EM Huygensov izvor:



$\vec{E}_0 = \vec{a}_x E_0$

$\vec{H}_0 = \vec{a}_y \frac{E_0}{Z_0}$

$\vec{K} = \vec{a}_n \times \vec{H}_0 = -\vec{a}_x \frac{E_0}{Z_0}$

$\vec{K}_m = \vec{E}_0 \times \vec{a}_n = -\vec{a}_y E_0$

$$\vec{E} \cdot \vec{a}_s = \frac{1}{I_s l_s} \int_A (\vec{E}_s \cdot \vec{K} - \vec{H}_s \cdot \vec{K}_m) dA = \frac{jk}{4\pi} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} [\vec{a}_\theta \cdot (-\vec{a}_x) - \vec{a}_\phi \cdot (-\vec{a}_y)]$$

$$\vec{a}_\theta \cdot \vec{a}_x = -\cos\theta \cos\phi$$

$$\vec{a}_\phi \cdot \vec{a}_y = \cos\phi$$

$$E_\theta = \frac{j}{2\lambda} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} (\cos\theta + 1) \cos\phi$$

$$\vec{a}_\theta \cdot \vec{a}_x = \sin\phi$$

$$\vec{a}_\phi \cdot \vec{a}_y = -\cos\theta \sin\phi$$

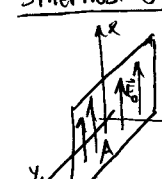
$$E_\phi = \frac{j}{2\lambda} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} (\cos\theta + 1) (-\sin\phi)$$

Polje EM Huygens:

$$\vec{E} = (\vec{a}_\theta \cos\phi - \vec{a}_\phi \sin\phi) \frac{j}{2\lambda} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} (\cos\theta + 1)$$

Enotni smernik = polarizacija v \vec{a}_x

Jakost izvora $F(\theta, \phi)$

Smernost odprtine na osi z ($\theta=0$):

$$D_{\text{max}}(\theta=0, \phi) = \frac{|\vec{S}_{\text{max}}|}{|\vec{S}_i|} = \frac{\frac{1}{2} E_0^2 \cos^2\theta}{\frac{1}{2} E_0^2} = \frac{4\pi r^2}{2 Z_0} \left| \int_A \frac{1}{2\lambda} E_0(x, y) \frac{1}{r} 2 dx dy \right|^2 = \frac{4\pi}{\lambda^2} \left| \int_A E_0(x, y) dx dy \right|^2$$

Fraunhofer ($\theta=0$) $\rightarrow e^{-jkr} \approx e^{-jkr} = \text{konst.}$

Zgled: $E_0(x, y) = \text{konst.} \rightarrow \text{max } D$

$$D = \frac{4\pi}{\lambda^2} \frac{|E_0|^2 A^2}{|E_0|^2 A} = \frac{4\pi}{\lambda^2} A$$

Poljubna $E_0(x, y)$:

$$D = \frac{4\pi}{\lambda^2} A_{\text{eff}} = \frac{4\pi}{\lambda^2} \eta_0 A$$

Izkoristek osvetlitve:

$$\eta_0 = \frac{\left| \int_A E_0(x, y) dx dy \right|^2}{A \int_A |E_0(x, y)|^2 dx dy}$$

Efektivna površina:

$$A_{\text{eff}} = \frac{\left| \int_A E_0(x, y) dx dy \right|^2}{\int_A |E_0(x, y)|^2 dx dy}$$

Antene in razširjanje valov #5

29. 10. 2013

Huygens-ov izvor:

v ravnini xy, sevanje v smeri +z

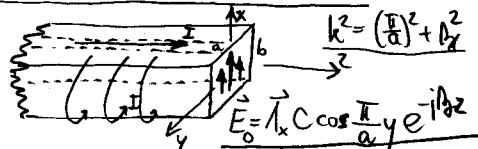
$$d\vec{E} = (\vec{I}_0 \cos \phi - \vec{I}_0 \sin \phi) \frac{j}{2\lambda} E_0(x,y) dx dy \frac{e^{jkr}}{r} (\cos \theta + 1) @ \vec{E}_0 = \vec{I}_x E_0$$

$$d\vec{E} = (\vec{I}_0 \sin \phi + \vec{I}_0 \cos \phi) \frac{j}{2\lambda} E_0(x,y) dx dy \frac{e^{jkr}}{r} (\cos \theta + 1) @ \vec{E}_0 = \vec{I}_y E_0$$

Max smernost, Aeff, η_0 : $A_{eff} = A \eta_0$

$$D = \frac{4\pi | \int_A E_0(x,y) dx dy |^2}{\lambda^2 \int_A |E_0(x,y)|^2 dx dy} = \frac{4\pi}{\lambda^2} A_{eff}$$

Pravokotni kovinski valovod:



$$\lambda_g = \frac{2\pi}{\beta}$$

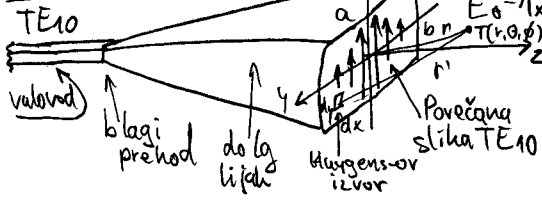
Izkoristek osvetlitve $\vec{E} = \vec{I}_x \cos \frac{\pi}{a} y$

$$\eta_0 = \frac{| \int_A C \cos \frac{\pi}{a} y dx dy |^2}{A \int_A |C \cos \frac{\pi}{a} y|^2 dx dy} = \frac{|C|^2 a^2 b^2 \frac{4}{\pi^2}}{|C|^2 a^2 b^2 \frac{1}{2}} = \frac{8}{\pi^2}$$

$$\eta_0 \approx 82\%$$

$$Zgled: a = \lambda, b = \frac{\lambda}{2} \rightarrow D = \frac{16}{\pi} \approx 5$$

Piramidni lijak



$$\vec{E}_0 = \vec{I}_x C \cos \frac{\pi}{a} y \quad d\vec{E} = (\vec{I}_0 \cos \phi - \vec{I}_0 \sin \phi) \frac{j}{2\lambda} C \cos \frac{\pi}{a} y dx dy \frac{e^{jkr}}{r} (1 + \cos \theta)$$

Fraunhofer: $r > \frac{2a^2}{\lambda} \rightarrow$ zanemarimo amplitude ϕ, ϕ', r'
 $\cos \theta_x = \sin \theta \cos \phi \quad \cos \theta_y = \sin \theta \sin \phi$ POMEMBNA FAZA $e^{jkr'} \approx e^{jkr} e^{j k x \cos \theta_x} e^{j y \cos \theta_y}$

$$r' = \sqrt{(r \sin \theta \cos \phi - x)^2 + (r \sin \theta \sin \phi - y)^2 + (r \cos \theta)^2} \approx r - x \cos \theta_x - y \cos \theta_y$$

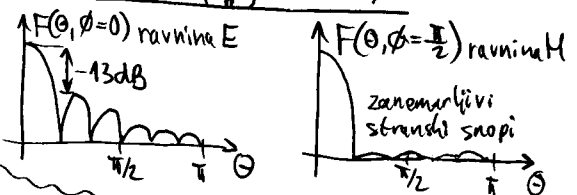
$$\vec{E} = \int_{-\frac{a}{2}}^{+\frac{a}{2}} \int_{-\frac{b}{2}}^{+\frac{b}{2}} d\vec{E} = (\vec{I}_0 \cos \phi - \vec{I}_0 \sin \phi) \frac{jC}{2\lambda} \frac{e^{jkr}}{r} \int_{-\frac{a}{2}}^{+\frac{a}{2}} \cos \frac{\pi}{a} y e^{j k y \cos \theta_y} dy \int_{-\frac{b}{2}}^{+\frac{b}{2}} e^{-j k x \cos \theta_x} dx (1 + \cos \theta)$$

$$I_x = \int_{-\frac{b}{2}}^{+\frac{b}{2}} e^{j k x \cos \theta_x} dx = \frac{e^{j k x \cos \theta_x}}{j k \cos \theta_x} \Big|_{-\frac{b}{2}}^{+\frac{b}{2}} = \frac{2 \sin(\frac{kb}{2} \cos \theta_x)}{j k \cos \theta_x} \cdot \frac{b}{2} = b \cdot \frac{\sin(\frac{kb}{2} \sin \theta \cos \phi)}{\frac{kb}{2} \sin \theta \cos \phi}$$

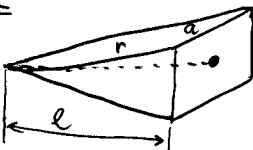
$$I_y = \int_{-\frac{a}{2}}^{+\frac{a}{2}} \cos \frac{\pi}{a} y e^{j k y \cos \theta_y} dy = \frac{1}{2} \int_{-\frac{a}{2}}^{+\frac{a}{2}} [e^{j(k \cos \theta_y + \frac{\pi}{a})y} + e^{j(k \cos \theta_y - \frac{\pi}{a})y}] dy = \frac{2j \sin(\frac{ka}{2} \cos \theta_y + \frac{\pi}{2})}{2j(k \cos \theta_y + \frac{\pi}{a})} + \frac{2j \sin(\frac{ka}{2} \cos \theta_y - \frac{\pi}{2})}{2j(k \cos \theta_y - \frac{\pi}{a})}$$

$$= \frac{\cos(\frac{ka}{2} \cos \theta_y)}{k \cos \theta_y + \frac{\pi}{a}} - \frac{\cos(\frac{ka}{2} \cos \theta_y)}{k \cos \theta_y - \frac{\pi}{a}} = \frac{2 \frac{\pi}{a} \cos(\frac{ka}{2} \cos \theta_y)}{(\frac{\pi}{a})^2 - k^2 \cos^2 \theta_y} \cdot (\frac{a}{\pi})^2 = a \cdot \frac{2}{\pi} \cdot \frac{\cos(\frac{ka}{2} \sin \theta \sin \phi)}{1 - (\frac{ka}{\pi})^2 \sin^2 \theta \sin^2 \phi}$$

$$F(\theta, \phi) = (1 + \cos \theta) \frac{\sin(\frac{kb}{2} \sin \theta \cos \phi)}{\frac{kb}{2} \sin \theta \cos \phi} \cdot \frac{\cos(\frac{ka}{2} \sin \theta \sin \phi)}{1 - (\frac{ka}{\pi})^2 \sin^2 \theta \sin^2 \phi}$$



kroglaste fronte = kvadratna napaka faze

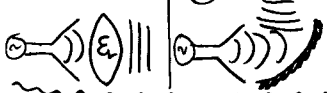


$$r = \sqrt{\lambda^2 + (\frac{a}{2})^2 + (\frac{b}{2})^2}$$

$$\Delta \phi = k(r-l) \approx k \frac{a^2 + b^2}{8l} = \frac{\pi(a^2 + b^2)}{4l\lambda}$$

Popravek faze:

1) LEČA 2) ZRCALO



3) SKUPNJA



$\Delta \phi$	ΔG
$\frac{2\pi}{\lambda}$	-0 dB
$\frac{\pi}{\lambda}$	-4 dB
$\frac{\pi/4}{\lambda}$	-1 dB
$\frac{\pi/8}{\lambda}$	-0.5 dB

$$\frac{\pi}{2} = \frac{\pi(a^2 + b^2)}{4l\lambda}$$

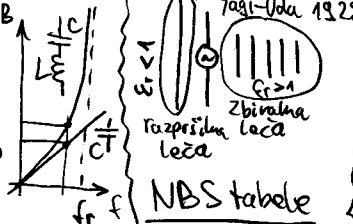
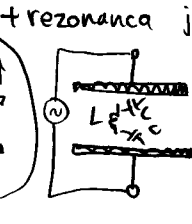
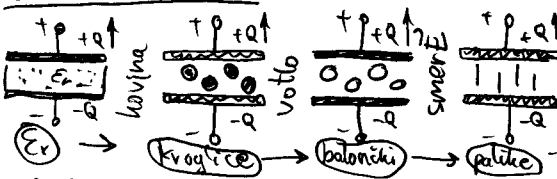
$$l = \frac{a^2 + b^2}{2\lambda}$$

$$Zgled: f = 126 \text{ MHz} \rightarrow \lambda = 2.5 \text{ cm}$$

$$a = b = 50 \text{ cm}$$

$$l = \frac{2500 \text{ cm}^2 + 2500 \text{ cm}^2}{2 \cdot 2.5 \text{ cm}} = 10 \text{ m!}$$

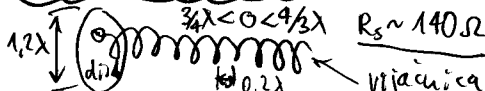
Umetni dielektrik:



SLOW-WAVE STRUCTURE

||||| palčke
 XXXXX križci 2x pol
 OOOOO zavlece
 UUUU U-ji VVVV
 NNNN N-ji LLLL
 ●●●●● diski

Vijačna antena z osnim sevanjem



$3\lambda/4 < \alpha < 9/8\lambda$
 $R_s \sim 140 \Omega$
 darna = RHCP
 leva = LHCP

Antene in razširjanje valov #6 5/11/2013

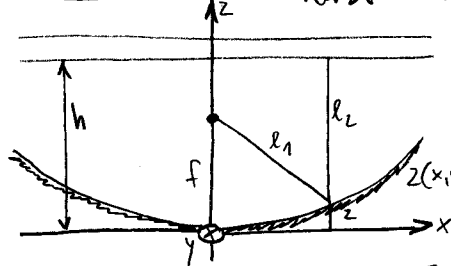
Oblika zrcala:

konst = $l_1 + l_2 = f + h = \sqrt{x^2 + y^2 + (f-z)^2} + h - z$

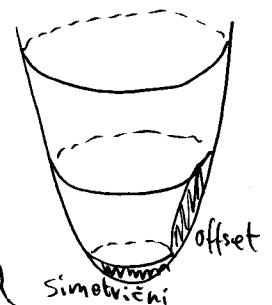
$l_1 = \sqrt{x^2 + y^2 + (f-z)^2}$ $\sqrt{x^2 + y^2 + (f-z)^2} = f + z$

$l_2 = h - z$ $x^2 + y^2 + f^2 - 2fz + z^2 = f^2 + 2fz + z^2$

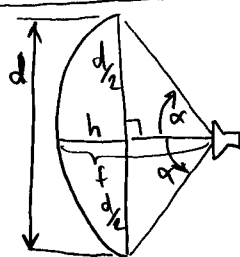
$x^2 + y^2 = 4fz \rightarrow z(x, y) = \frac{x^2 + y^2}{4f}$



12vez



Simetrično zrcalo:



$$f = \frac{d^2}{16h}$$

$$\alpha = \arctg \frac{d/2}{f-h}$$

$$\alpha = \arctg \frac{1}{2f/d - \frac{1}{8f/d}}$$

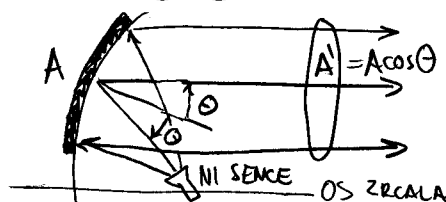
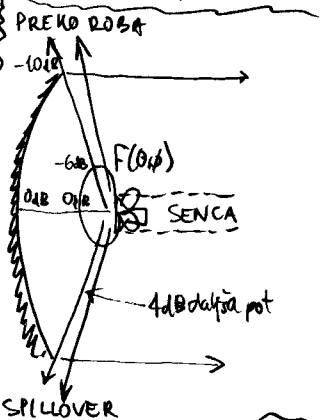
$f/d = 0.3 \dots 0.4$ (zaslonka fotoaparata)

$f/d = 0.4 \rightarrow \alpha = 64^\circ; 2\alpha = 128^\circ$

SENCA ŽARILCA $\rightarrow d > 5\lambda$

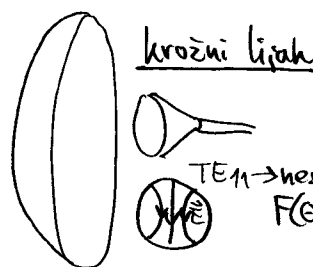
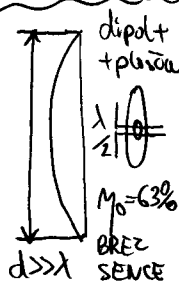
OSVETLITEV ROBA

$-6dB F(\theta, \phi) - 4dB$ daljša pot



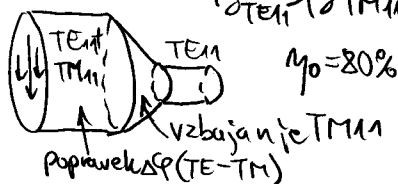
Offset zrcalo:

$f/d = 0.6 \dots 0.7$

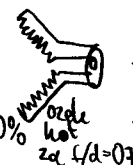
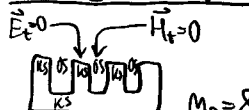


Dvorodovni: lijak $TE_{11} + TM_{11}$

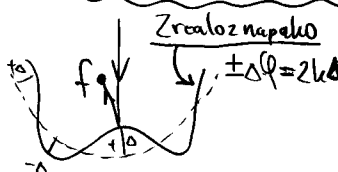
$\beta_{TE_{11}} > \beta_{TM_{11}}$



Korugirani lijak

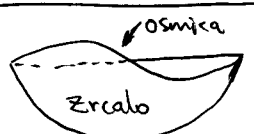


Širok kot za $f/d = 0.3 \dots 0.4$

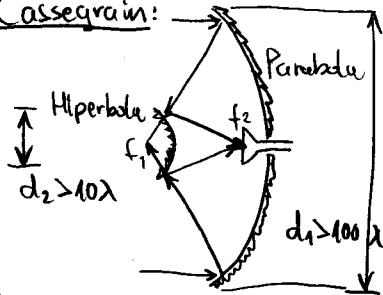


$\pm \Delta \phi$	ΔG	$\pm \Delta$
$\pm \pi$	$-\infty$	$\pm \lambda/4$
$\pm \pi/2$	$-4dB$	$\pm \lambda/8$
$\pm \pi/4$	$-1dB$	$\pm \lambda/16$
$\pm \pi/8$	$-0.25dB$	$\pm \lambda/32$

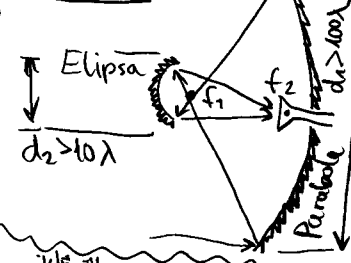
$f = 12GHz \rightarrow \pm \lambda/32 = \pm 0.8mm$



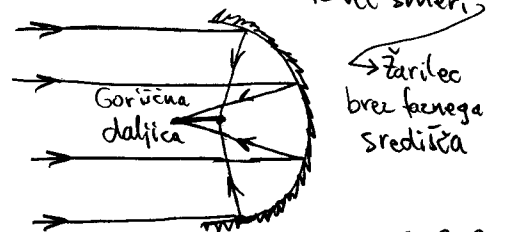
Cassegrain:



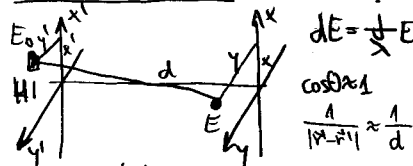
Gregorian:



Krogno zrcalo \rightarrow istočasni sprejem iz več smeri



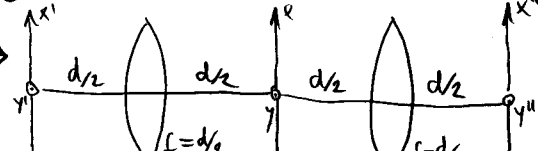
2D-Fourier:



$$dE = \frac{1}{x} E_0(k', y') \frac{e^{-ik'f - F1}}{1F - F1} dx' dy'$$

$$\cos \theta \approx 1$$

$$E = \frac{1}{x} \frac{e^{-ikd}}{d} e^{-ik \frac{x^2 + y^2}{2d}} \iint E_0(k', y') e^{-ik' \frac{x^2 + y^2}{2d}} e^{-ik' \frac{x^2}{2d}} e^{-ik' \frac{y^2}{2d}} dx' dy'$$



Fourier

prozoren diapozitiv brez faze modulacije

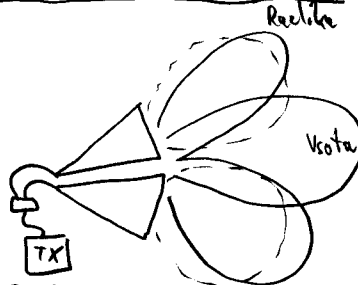
istoza prostorske frekvence

LPP HPP

Koherentna skupina



Sestevanje kazalcev polja!



Pravilo o množenju F(θ, φ)

- 1 ENAKE ANTENE
 - 2 ENAKO ORIENTIRANE
 - 3 ENAKO POLARIZIRANE
- $F(\theta, \phi) = F_e(\theta, \phi) \cdot F_s(\theta, \phi)$
 $D \neq D_e \cdot D_s$ NE VELJA!

DVA ZOBODRŽNA VIRA

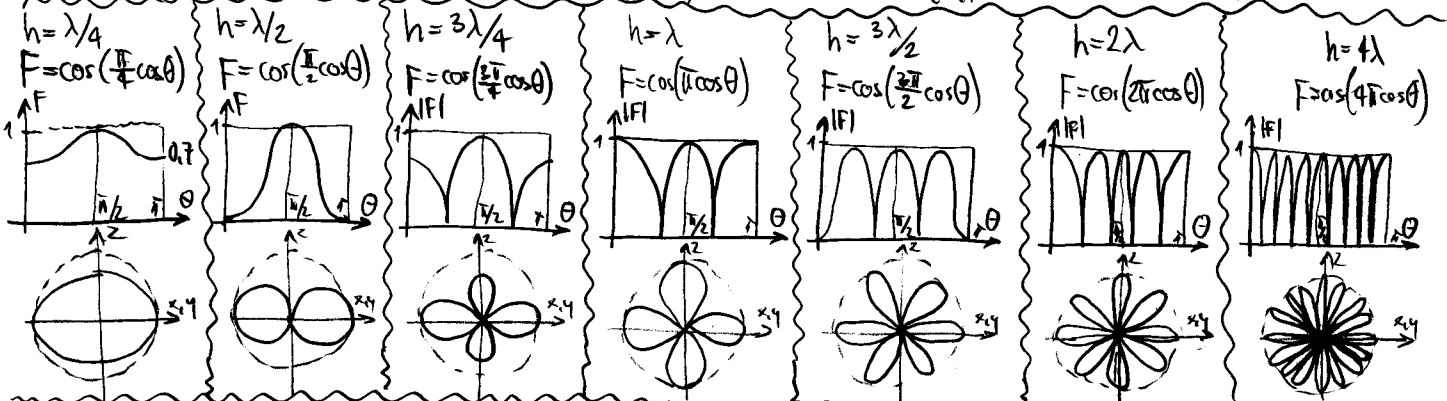
$\vec{E} = \vec{E}_1 + \vec{E}_2$
 $\vec{E} = \vec{E}_1 \propto I_1 \frac{e^{-jkr_1}}{r_1} + \vec{E}_2 \propto I_2 \frac{e^{-jkr_2}}{r_2}$
 Fraunhofer $r > \frac{2h^2}{\lambda}$; $\vec{E}_1 = \vec{E}_2 = \vec{E}$; $\frac{1}{r_1} = \frac{1}{r_2} = \frac{1}{r}$
 $r_1 = \sqrt{r^2 + (h/2)^2 - rh \cos \theta} \approx r - \frac{h}{2} \cos \theta$
 $r_2 = \sqrt{r^2 + (h/2)^2 + rh \cos \theta} \approx r + \frac{h}{2} \cos \theta$

$\vec{E} = \vec{E}_0 \propto \frac{e^{-jkr}}{r} (I_1 e^{j\frac{kh}{2} \cos \theta} + I_2 e^{-j\frac{kh}{2} \cos \theta})$

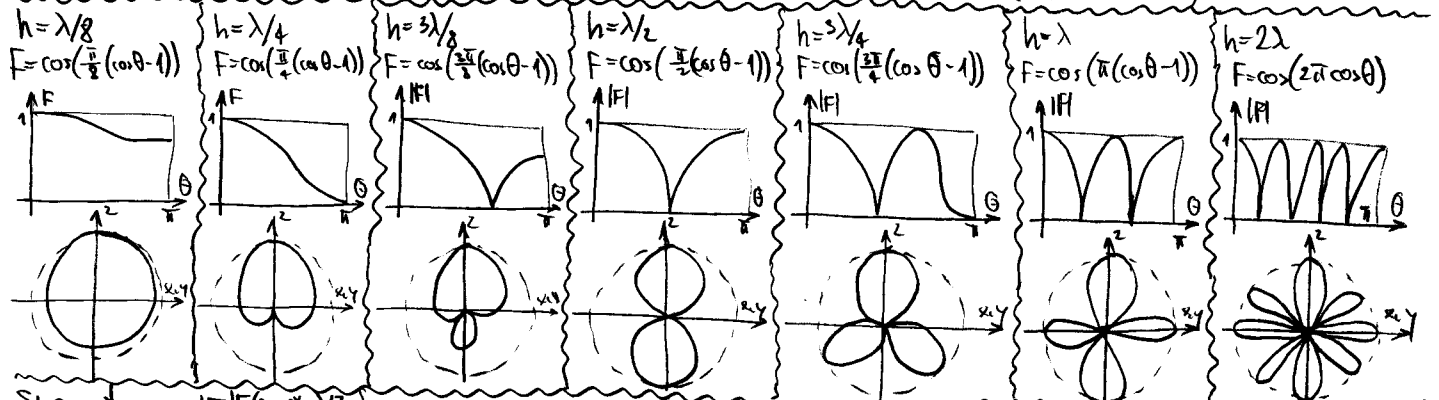
Najzanimivejši primer: $|I_1| = |I_2| \rightarrow I_1 = I_0 e^{j\frac{\pi}{2}}; I_2 = I_0 e^{-j\frac{\pi}{2}}$
 $\vec{E} = \vec{E}_0 I_0 \propto \frac{e^{-jkr}}{r} (e^{j(\frac{\pi}{2} + \frac{kh}{2} \cos \theta)} + e^{-j(\frac{\pi}{2} + \frac{kh}{2} \cos \theta)})$

$\vec{E} = \vec{E}_0 I_0 \propto \frac{e^{-jkr}}{r} 2 \cos(\frac{\pi}{2} + \frac{kh}{2} \cos \theta) \rightarrow F(\theta, \phi) = \cos(\frac{\pi}{2} + \frac{kh}{2} \cos \theta)$

Bočna skupina $\varphi = 0 \rightarrow F(\theta, \phi) = \cos(\frac{kh}{2} \cos \theta)$; $k = \frac{2\pi}{\lambda} \rightarrow F(\theta, \phi) = \cos(\pi \frac{h}{\lambda} \cos \theta)$



Osnovna skupina: $\varphi = -kh$ možna izbira $\rightarrow F(\theta, \phi) = \cos(\frac{kh}{2} (\cos \theta - 1)) = \cos(\pi \frac{h}{\lambda} (\cos \theta - 1))$



Smernost: $D = \frac{4\pi |F(\theta_m, \phi_m)|^2}{\int |F(\theta, \phi)|^2 d\Omega}$

$D = \frac{4\pi |F(\theta_m, \phi_m)|^2}{2\pi \int_0^\pi \cos^4(\frac{\pi}{2} + \frac{kh}{2} \cos \theta) \sin \theta d\theta}$

$D = \frac{2 |F(\theta_m, \phi_m)|^2}{\int_0^\pi (1 + \cos(\pi(1 + \frac{h}{\lambda} \cos \theta))) d\theta}$

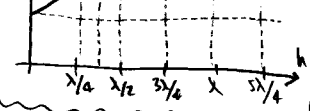
$D = \frac{2 |F(\theta_m, \phi_m)|^2}{1 + \frac{\sin kh}{kh} \cos \varphi}$

Osnovna max D: $\varphi \rightarrow \pi$
 $h \rightarrow 0 \rightarrow R_s?$

Bočna: $\varphi = 0, F(\theta_m, \phi_m) = 1$



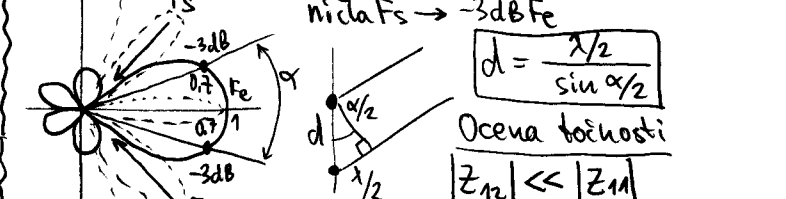
Osnovna: $\varphi = -kh, |F(\theta_m, \phi_m)| = 1$



$|F(\theta_m, \phi_m)| \ll 1$
 $D_{max} \rightarrow 4$

$P_s = 4P_{s1}$ $P_g = |I|^2 \text{Re}[Z_{11} + Z_{12}]$
 $P_{g1} = \frac{1}{2} |I|^2 \text{Re}[Z_{11}]$
 $D = D_e \frac{P_s}{P_{s1}} \frac{P_{g1}}{P_g} = D_e \frac{2 \text{Re}[Z_{11}]}{\text{Re}[Z_{11} + Z_{12}]}$

Priljubeno pravilo: stranski snop $F_s \rightarrow$ ničla $F_e!!!$
 ničla $F_s \rightarrow -3\text{dB } F_e$

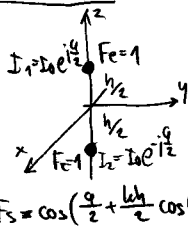


Antene in razširjanje valov

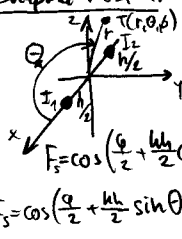
8

19/11/2013

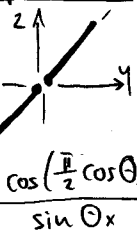
Ponovitev:



Skupina v osi X:



1/2 dipol v osi X:



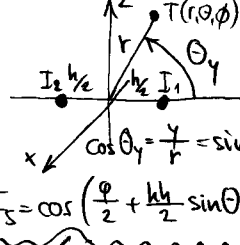
$$\cos \theta_x = \sin \theta \cos \phi = \frac{x}{r}$$

$$\sin \theta_x = \pm \sqrt{1 - \cos^2 \theta_x}$$

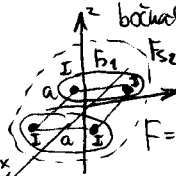
$$\sin \theta_x = \pm \sqrt{1 - \sin^2 \theta \cos^2 \phi}$$

$$F = \frac{\cos(\frac{\omega}{2} \cos \theta_x)}{\sin \theta_x} = \frac{\cos(\frac{\omega}{2} \sin \theta \cos \phi)}{\sqrt{1 - \sin^2 \theta \cos^2 \phi}}$$

Skupina v osi Y:



Oglednica kvadrata XY:



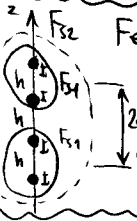
Fe=1

$$F_{S1} = \cos(\frac{k a}{2} \sin \theta \sin \phi)$$

$$F_{S2} = \cos(\frac{k a}{2} \sin \theta \cos \phi)$$

$$F = \cos(\frac{k a}{2} \sin \theta \cos \phi) \cos(\frac{k a}{2} \sin \theta \sin \phi)$$

bočina \phi=0

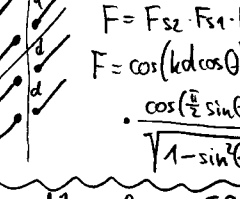


$$F_{S1} = \cos(\frac{k d}{2} \cos \theta)$$

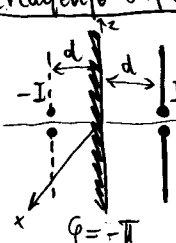
$$F_{S2} = \cos(\frac{k d}{2} \cos \theta)$$

$$F = \cos(k d \cos \theta) \cos(\frac{k d}{2} \cos \theta)$$

4 dipoli v X na osi Z:



Zrcaljenje dipola



Fe=1

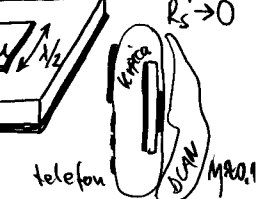
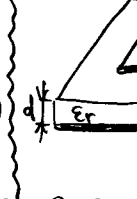
$$F_{S1} = \cos(-\frac{\omega}{2} + k d \sin \theta \sin \phi)$$

$$F_{S2} = \sin(k d \sin \theta \sin \phi)$$

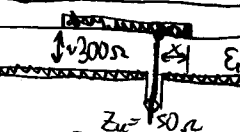
$$F = \sin(k d \sin \theta \sin \phi) \cos(\frac{\omega}{2} \cos \theta)$$

Mikrostrijska korpica

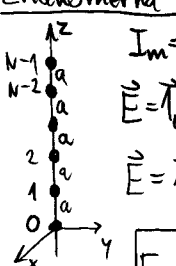
$$k d \ll 1 \rightarrow \sin(k d \cos \theta_y) \ll 1 \rightarrow M \ll 1$$



Prilagoditev R_s na 50 \Omega



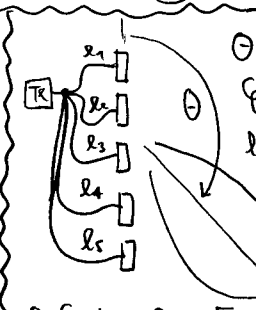
Enakomerna skupina



Frankhofer samo faza:

$$\vec{E}_0 = \vec{E} \propto \frac{e^{-jkr}}{r}$$

Frankhofer samo faza:



\theta > \frac{\pi}{2} Električni odklon navzdol

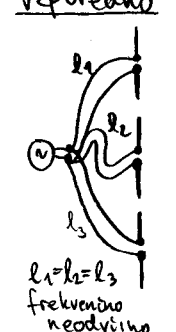
$$\phi = -k a \cos \theta > 0$$

$$l_1 < l_2 < l_3 < l_4 < l_5$$

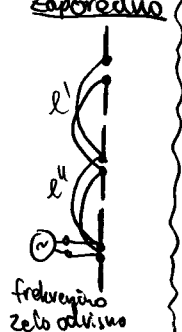
Napačen ukrep!



Vzoredno

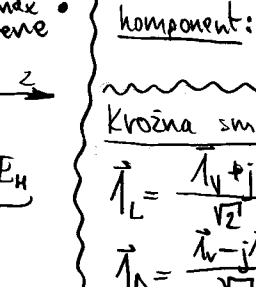


Zaporedno



Polarizacija: K Svezan!

na F_max antene



Razmerje linearnih komponent:

$$\frac{E_v}{E_h} \equiv \text{dva podatka polarizacije}$$

(odvisna od izbire \vec{r}_v!)

$$E_v = \vec{r}_v \cdot \vec{E} \quad E_h = \vec{r}_h \cdot \vec{E}$$

Krožna smernika (IEEE):

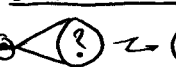
$$\vec{r}_L \cdot \vec{r}_L^* = 1; \vec{r}_L \cdot \vec{r}_D^* = 0$$

$$\vec{r}_L = \frac{\vec{r}_v + j \vec{r}_h}{\sqrt{2}}$$

$$\vec{r}_D = \frac{\vec{r}_v - j \vec{r}_h}{\sqrt{2}}$$

$$Q = \frac{E_L}{E_D} \equiv \text{razmerje krožnih komponent}$$

Osnovne razmerje:



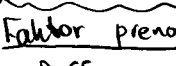
$$\frac{U_{max}}{U_{min}} = R$$

$$1 \leq R = \left| \frac{1 + |Q|}{1 - |Q|} \right|$$

$$R_{dB} = 20 \log R$$

R in |Q| neodvisna od \vec{r}_v!

Faktor prenosa moči:



$$P_s = P_0 G_0 \left(\frac{\lambda}{4\pi r} \right)^2 \frac{1 + |Q_0|^2}{(1 + |Q_0|^2)(1 + |Q_s|^2)}$$

$$0 \leq \eta \leq 1$$

Polarizacija	Q	R	Faktor \eta							
			VP	HP	RHCP	LHCP	PP45	PP45	PP45	PP45
VP	1	\infty	1	0	1/2	1/2	1/2	1/2	1/2	1/2
HP	-1	\infty	0	1	1/2	1/2	1/2	1/2	1/2	1/2
RHCP	0	1	1/2	1/2	1	0	1/2	1/2	1/2	1/2
LHCP	\infty	1	1/2	1/2	0	1	1/2	1/2	1/2	1/2
PP45	-j	\infty	1/2	1/2	1/2	1/2	0	1	1	0
PP45	+j	\infty	1/2	1/2	1/2	1/2	1	0	0	1

Krožno-polarizirane antene

90° fazni zamik

2 anteni pod pravim kotom

→ napajanje l = \lambda/4

→ napajanje R+C, R+L

→ dipoli različnih dolžin

→ obrezana hrpica

→ eliptični valvod \Delta \beta

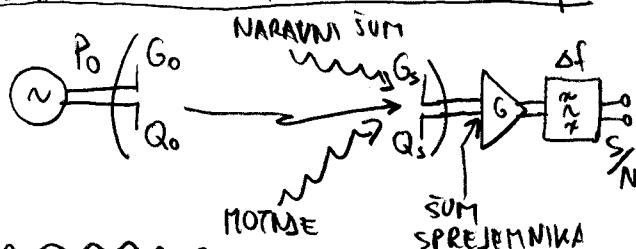
→ vijaki pod 45°, ploščica \epsilon_r

→ dvodomni dielektrik

→ vijakna antena z osnim senčjem

→ spiralna antena

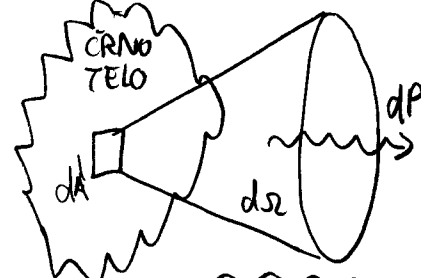
Kohherentna zveza, nekohherentne matrice



Spektralna svetlost

$$B_f = \frac{dP}{df dA' d\Omega}$$

$$B_\lambda = \frac{dP}{d\lambda dA' d\Omega}$$



Planck-ov zakon

(ČRNO TELO)

$$B_f = \frac{2hf^3}{c^2} \frac{1}{e^{\frac{hf}{k_B T}} - 1}$$

$$h = 6.625 \cdot 10^{-34} \text{ Js}$$

$$k_B = 1.38 \cdot 10^{-23} \text{ J/K}$$

$$c_0 = 3 \cdot 10^8 \text{ m/s}$$

Rayleigh-Jeans

Približek $hf \ll k_B T$

$$e^{\frac{hf}{k_B T}} - 1 \approx \frac{hf}{k_B T}$$

$$B_f = \frac{2k_B T f^2}{c^2}$$

$$B_\lambda = \frac{2k_B T}{\lambda^2}$$

Wien

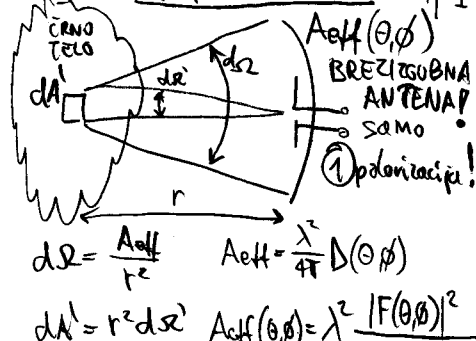
Približek $hf \gg k_B T$

$$B_f = \frac{2hf^3}{c^2} e^{-\frac{hf}{k_B T}}$$

$$f = 100 \text{ GHz}, T = 300 \text{ K}$$

$$\frac{hf}{k_B T} = \frac{6.625 \cdot 10^{-34} \text{ Js} \cdot 10^5 \text{ s}^{-1}}{1.38 \cdot 10^{-23} \text{ J/K} \cdot 300 \text{ K}} \approx 0.016$$

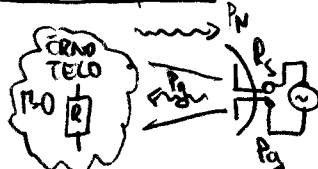
Sprejeta moč šuma



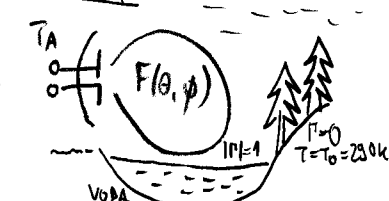
$$P_N = \frac{1}{2} \int B_f df d\Omega dA' = \frac{df}{2} \int_{4\pi} B_f \frac{A_{eff}}{r^2} r^2 d\Omega = \frac{df}{2} \int_{4\pi} B_\lambda \lambda^2 \frac{|F(\theta, \phi)|^2}{\int_{4\pi} |F(\theta, \phi)|^2 d\Omega} d\Omega = \frac{df \lambda^2}{2} \frac{\int_{4\pi} B_\lambda(\theta, \phi) |F(\theta, \phi)|^2 d\Omega}{\int_{4\pi} |F(\theta, \phi)|^2 d\Omega}$$

$$\text{Rayleigh-Jeans: } B_f(\theta, \phi) = \frac{2k_B T}{\lambda^2} T(\theta, \phi) \rightarrow P_N = df k_B \frac{\int_{4\pi} T(\theta, \phi) |F(\theta, \phi)|^2 d\Omega}{\int_{4\pi} |F(\theta, \phi)|^2 d\Omega} ; T_A = \frac{\int_{4\pi} T(\theta, \phi) |F(\theta, \phi)|^2 d\Omega}{\int_{4\pi} |F(\theta, \phi)|^2 d\Omega} \cdot P_N = df k_B T_A$$

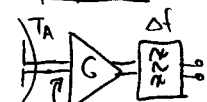
Sevalna upornost



Sum okolja



Sprejemnik:



$$P_N = \Delta f k_B (T_A + T_s)$$

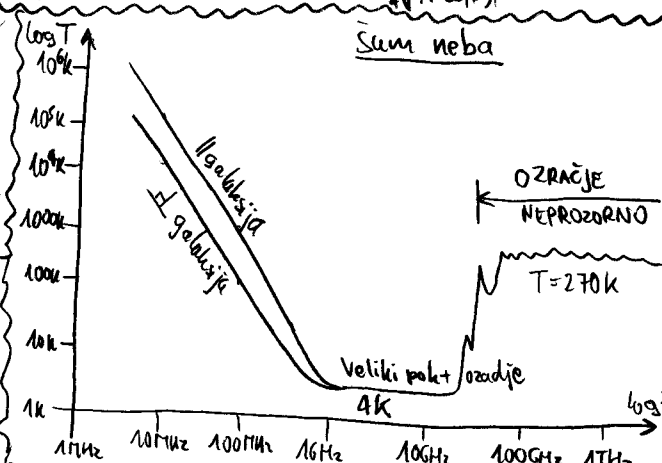
Polprevodniki $T_s = 30 \text{ K} - 300 \text{ K}$ Cel sprejemnik $T_s = 100 \text{ K} - 1000 \text{ K}$ Zgled: GSM telefon $S/N = 10 \text{ dB}$

$$\Delta f = 200 \text{ kHz}, T_A + T_s = 1000 \text{ K}$$

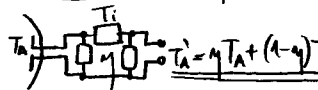
$$P_N = \Delta f \cdot k_B (T_A + T_s) = 2 \cdot 10^5 \text{ s}^{-1} \cdot 1.38 \cdot 10^{-23} \text{ J/K} \cdot 1000 \text{ K} = 2.76 \cdot 10^{-15} \text{ W}$$

$$P_s = S/N \cdot P_N = 2.76 \cdot 10^{-14} \text{ W}$$

$$P_s [\text{dBm}] = 10 \log \frac{P_s}{1 \text{ mW}} \approx -106 \text{ dBm}$$



$$k_B T_0 = 1.38 \cdot 10^{-23} \text{ J/K} \cdot 2.73 \text{ K} = 4 \cdot 10^{-24} \text{ W s} = -174 \text{ dBm/Hz}$$

Izgubna antena $\eta < 1$ 

$$T_A = \eta T_s + (1 - \eta) T_l$$

$$T_N = 10 \text{ K}, \text{ Zgled GPSRX: } F = 1 + \cos \theta$$

$$\mu = \cos \theta$$

$$T_2 = 290 \text{ K}$$

$$T_A = \frac{\int_{4\pi} T(\theta) (1 + \cos \theta)^2 d\Omega}{\int_{4\pi} (1 + \cos \theta)^2 d\Omega}$$

$$T_A = \frac{T_N \int_{-1}^1 (1 + \mu)^2 d\mu + T_2 \int_{-1}^1 (1 + \mu)^2 d\mu}{\int_{-1}^1 (1 + \mu)^2 d\mu}$$

$$T_A = 45 \text{ K}$$

Antena v Sonce:

$$T_s \sim 10^6 \text{ K} @ 1.5 \text{ GHz}$$

$$T_N \sim 10 \text{ K}$$

$$\Omega_s \ll \Omega_A$$

$$D = 20 \text{ dB} = 100$$

$$F(\theta, \phi)$$

$$\alpha_s = 9.5 \text{ mrad}$$

$$\Omega = \frac{A}{r^2}$$

$$A = 2\pi r h$$

$$\Omega = 2\pi (1 - \cos(\alpha/2))$$

$$\Omega \approx \frac{\pi}{4} \alpha^2 [\text{rd}] = 64 \cdot 10^{-6} \text{ sr}$$

$$T_A = \frac{T_s \int_{\Omega_s} |F(\theta, \phi)|^2 d\Omega + T_N \int_{4\pi} |F(\theta, \phi)|^2 d\Omega}{\int_{4\pi} |F(\theta, \phi)|^2 d\Omega}$$

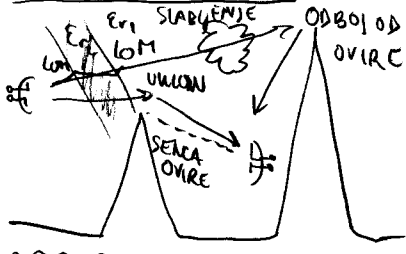
$$T_A \approx T_s \Omega_s \frac{|F(\theta, \phi)|^2}{\int_{4\pi} |F(\theta, \phi)|^2 d\Omega} + T_N$$

$$T_A \approx T_s \frac{\Omega_s}{4\pi} D + T_N$$

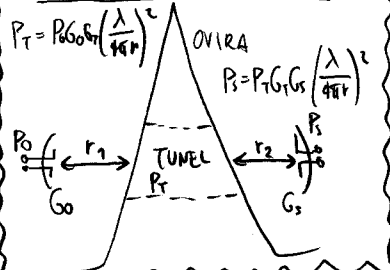
$$T_A = 10^6 \text{ K} \frac{64 \cdot 10^{-6} \text{ sr}}{4\pi} \cdot 100 + 10 \text{ K}$$

$$T_A = 506 \text{ K} + 10 \text{ K} = 516 \text{ K}$$

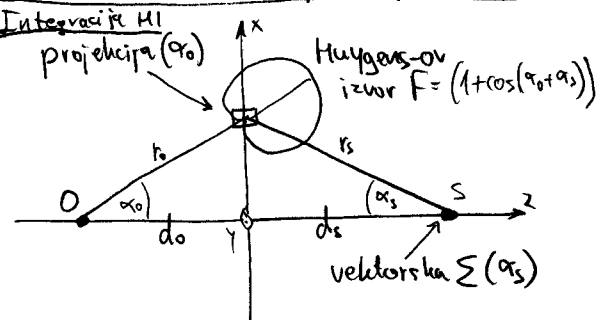
Notnje razširjanja:



2 zaporedni zvezi $\propto r^{-4}$



Integracija H1 projekcija (α_0)



$$E_0 = \alpha I \frac{e^{-ikr_0}}{r_0} \quad dE = \frac{1}{2\lambda} E_0 dx dy \frac{e^{-ikr_s}}{r_s} F(\alpha_0, \alpha_s)$$

$$r_0 = \sqrt{d_0^2 + x^2 + y^2} \approx d_0 + \frac{x^2 + y^2}{2d_0}$$

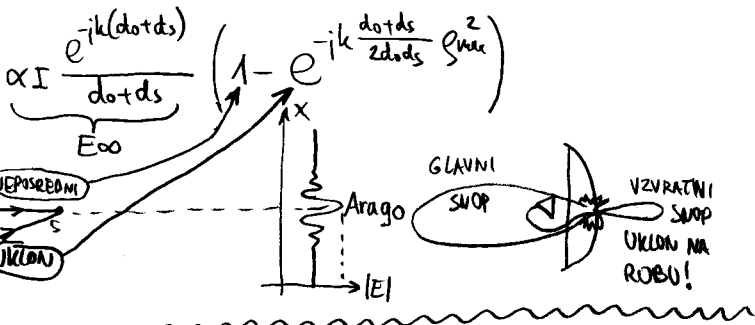
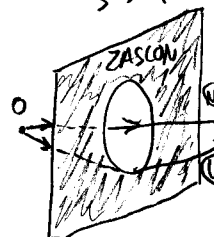
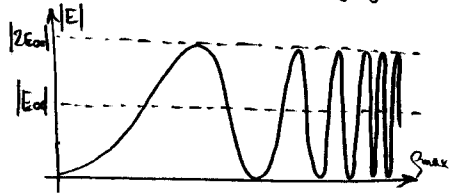
$$r_s = \sqrt{d_s^2 + x^2 + y^2} \approx d_s + \frac{x^2 + y^2}{2d_s}$$

$d_0, d_s \gg x, y \rightarrow$ povprečna amplituda: $\frac{1}{r_s} \approx \frac{1}{d_s}, \frac{1}{r_0} \approx \frac{1}{d_0}, F(\alpha_0, \alpha_s) \approx 2$

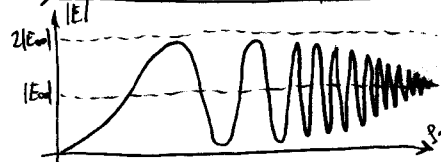
povprečni fazo: $e^{-ikr_0} \approx e^{-ikd_0} e^{-ik \frac{x^2 + y^2}{2d_0}}, e^{-ikr_s} \approx e^{-ikd_s} e^{-ik \frac{x^2 + y^2}{2d_s}}$

$$E = \iint_{x,y} \frac{1}{2\lambda} \alpha I \frac{e^{-ikr_0}}{r_0} dx dy \frac{e^{-ikr_s}}{r_s} F(\alpha_0, \alpha_s) \approx \frac{1}{2} \alpha I \frac{e^{-ik(d_0+d_s)}}{d_0 d_s} \iint_{x,y} e^{-ik \frac{d_0+d_s}{2d_0 d_s} (x^2 + y^2)} dx dy$$

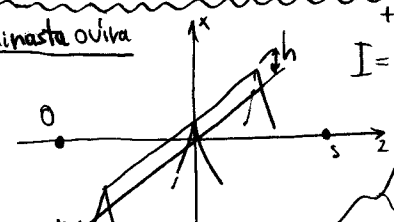
$$x, y \rightarrow \rho, \varphi \quad E = \frac{1}{2} \alpha I \frac{e^{-ik(d_0+d_s)}}{d_0 d_s} \int_0^{2\pi} \int_0^{\rho_{max}} e^{-ik \frac{d_0+d_s}{2d_0 d_s} \rho^2} \rho d\rho d\varphi = \alpha I \frac{e^{-ik(d_0+d_s)}}{d_0+d_s} \left(1 - e^{-ik \frac{d_0+d_s}{2d_0 d_s} \rho_{max}^2}\right)$$



ρ, φ z upoštevanjem amplitude

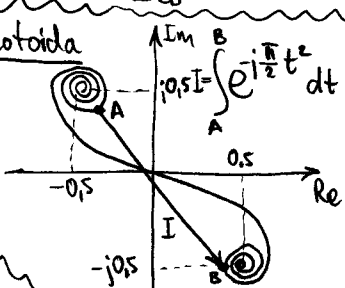


Klinasta ovira

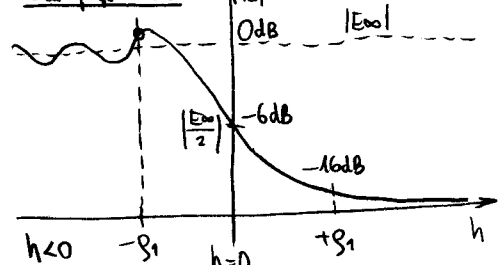


$$I = \int_h^{+\infty} e^{-ik \frac{d_0+d_s}{2d_0 d_s} x^2} dx \int_{-\infty}^{+\infty} e^{-ik \frac{d_0+d_s}{2d_0 d_s} y^2} dy$$

Klotoida

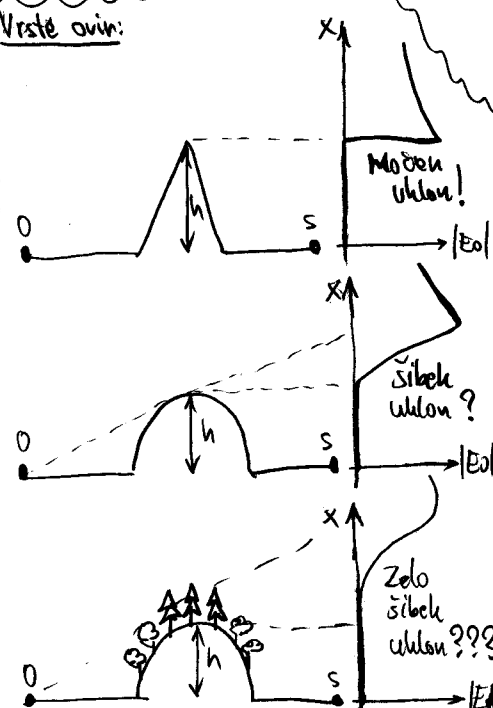


Slabljene ovire:

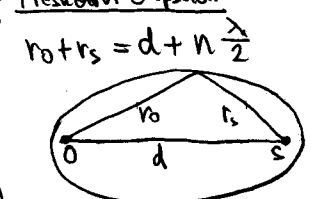


- $h < -s_1 \rightarrow a \approx 0dB$
- $h = 0 \rightarrow a = 6dB$
- $h > s_1 \rightarrow a = 16dB + 20 \log \frac{h}{s_1}$

Vrstne ovir:



Fresnelovi elipsoidi:

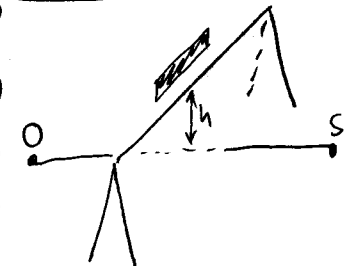


Polmeri FC:

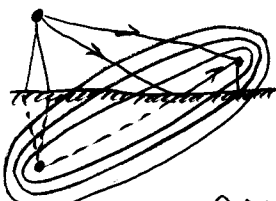
$$r_0 + r_s = d_0 + d_s + n \frac{\lambda}{2}$$

$$\rho_n = \sqrt{n \lambda \frac{d_0 d_s}{d_0 + d_s}}$$

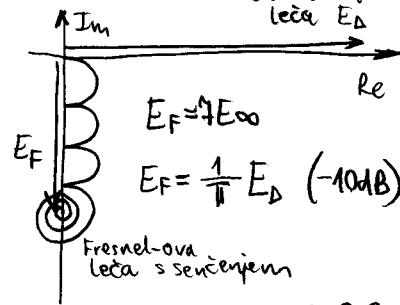
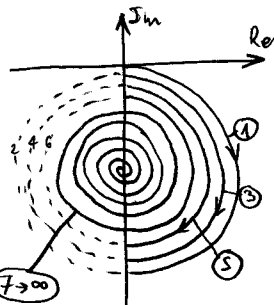
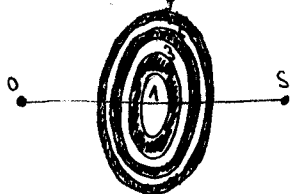
Uklanjalniki:



FC pri odboju:



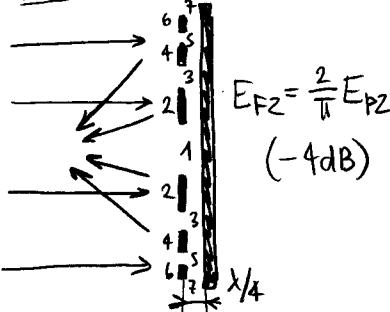
Fresnel-ova leća



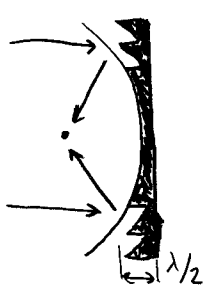
Fresnel-ova dielektrična:



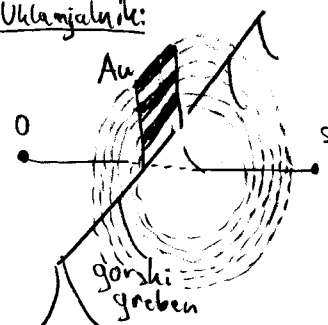
Fresnel-ovo zrcalo:



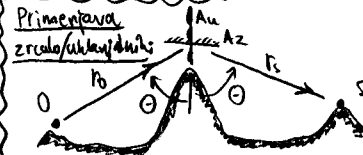
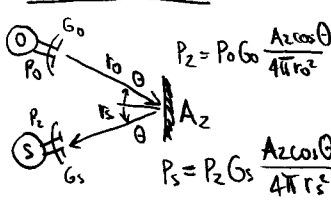
Fresnel-parabolično:



Uklanjalniki:

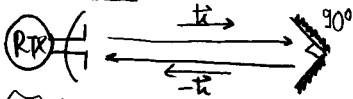


Ravno zrcalo:

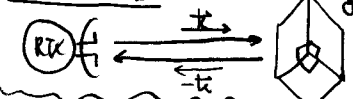


$$\frac{P_{su}}{P_{sz}} = \frac{A_u^2 \tan^2 \theta}{A_z^2 \frac{1}{\pi^2}}$$

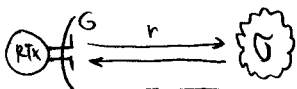
Vogel 2D:



Trirobnik 3D:



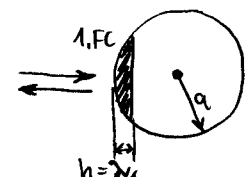
Odmerna površina:



$$P_s = P_o G^2 \frac{\lambda^2 G}{(4\pi)^3 r^4}$$

Ravna plošča (trirobnik) $G_e = \frac{4\pi}{\lambda^2} A^2$

Velike krogle $a \gg \lambda$:



$$G_{1FC} = \frac{4\pi}{\lambda^2} A_1^2 \left(\frac{2}{\pi}\right)^2$$

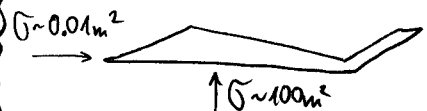
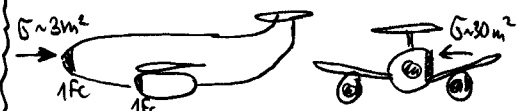
$$A_r = 2\pi a h$$

$$G_k = \frac{1}{4} G_{1FC}$$

$$G_k = \frac{1}{4} \frac{4\pi}{\lambda^2} (2\pi)^2 a^2 \left(\frac{1}{4}\right)^2 \left(\frac{2}{\pi}\right)^2$$

$$G_k = \pi a^2$$

Letala:



Domet radarja:

$$P_o = 10^6 W = 1 MW$$

$$P_s = 10^{-12} W = 1 pW$$

$$G = 40 dB (\sim 10 m^2)$$

$$\lambda = 0,1 m (3 GHz)$$

r = ?

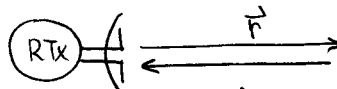
$$r = \sqrt{\frac{P_o}{P_s} \frac{G^2 \lambda^2}{(4\pi)^3} G}$$

$$G = 30 m^2 \rightarrow r = 350 km$$

$$G = 3 m^2 \rightarrow r = 197 km$$

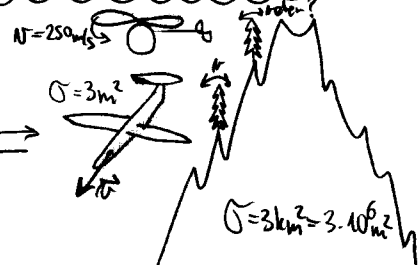
$$G = 0,01 m^2 \rightarrow r = 47 km$$

Doppler

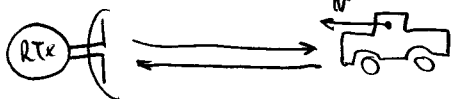


$$\Delta f = -2 f_o \frac{\vec{v} \cdot \vec{r}}{C_o}$$

$$|\vec{v} \cdot \vec{r}| > 40 m/s$$



Meritev hitrosti

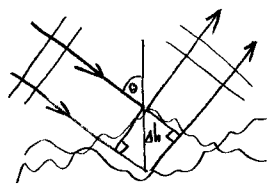
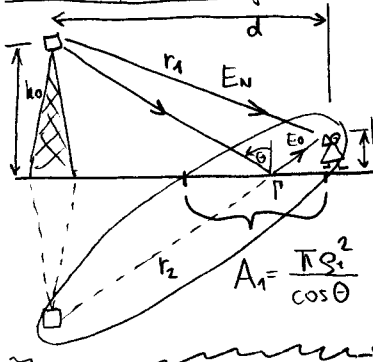


$$f_o = 246 Hz \rightarrow \lambda = 1,2 cm$$

$$f_o = 346 Hz \rightarrow \lambda = 0,9 cm$$

$$\Delta f = 2 f_o \frac{v}{C_o}$$

1. FC pri odboju

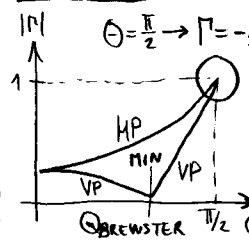


$$\Delta \varphi = 2k \sin \theta \cos \theta < \frac{\pi}{2}$$

za zrcalni odboj -1dB

Rayleigh-ov kriterij za
hrapavost: $\Delta h < \frac{\lambda}{8 \cos \theta}$

Odbojnost slabega dielektrika



$$E_s \approx \frac{\alpha I}{d} e^{-jk(d + \frac{h_0^2 + h_1^2}{2d})}$$

$$E_s = E_N + E_O$$

$$E_s = \alpha I \frac{e^{ikr_1}}{r_1} + \Gamma \alpha I \frac{e^{-ikr_2}}{r_2}$$

$$E_s \approx \frac{\alpha I}{d} [e^{ikr_1} + \Gamma e^{-ikr_2}]$$

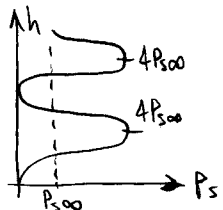
$$r_1 = \sqrt{d^2 + (h_0 - h_1)^2} \approx d + \frac{(h_0 - h_1)^2}{2d}$$

$$r_2 = \sqrt{d^2 + (h_0 + h_1)^2} \approx d + \frac{(h_0 + h_1)^2}{2d}$$

$$E_s \approx \frac{\alpha I}{d} [e^{ik \frac{h_0 h_1}{d}} - e^{-ik \frac{h_0 h_1}{d}}]$$

$$|E_s| \approx \frac{\alpha I}{d} 2 \sin(k \frac{h_0 h_1}{d})$$

$$P_s = P_0 G_0 G_s \left(\frac{\lambda}{4\pi d}\right)^2 4 \sin^2(k \frac{h_0 h_1}{d})$$



$h_0, h_1 \ll d$ VEKKE RAZBAJE

$$\sin(k \frac{h_0 h_1}{d}) \approx k \frac{h_0 h_1}{d} = 2\pi \frac{h_0 h_1}{\lambda d}$$

$$P_s = P_0 G_0 G_s \frac{h_0^2 h_1^2}{d^4}$$

Mestno okolje z ovirami:

$$P_s = P_0 G_0 G_s \frac{h_0^2 h_1^2}{d^4} \propto (\lambda)^{-4}; N=3 \dots 5$$

ZGLED: $\lambda = 33 \text{ cm}$

$$P_0 = 10 \text{ W} = +40 \text{ dBm}$$

$$P_s = 10^{-13} \text{ W} = -100 \text{ dBm}$$

$$G_0 = G_s = 1$$

$$h_0 = 1,5 \text{ m}$$

$$h_1 = 1,5 \text{ m} / 30 \text{ m}$$

$$d = ?$$

$$d = \sqrt[4]{\frac{P_0}{P_s} G_0 G_s h_0^2 h_1^2}$$

$$h_0 = 1,5 \text{ m} \rightarrow d = 4,74 \text{ km}$$

$$h_0 = 30 \text{ m} \rightarrow d = 21,2 \text{ km}$$

Primerjava prazen prostor:

$$d = \sqrt[4]{\frac{P_0}{P_s} G_0 G_s \left(\frac{\lambda}{4\pi}\right)^2} = 26,3 \text{ km}$$

OZRAČJE:

TROPOFERA 0-10 km

$$\epsilon = \epsilon_0 \epsilon_r, \gamma \neq 0$$

SUHI DEL ($N_2 + O_2$):

$$n = 1 + \Delta n_0 e^{-\frac{h}{H}}$$

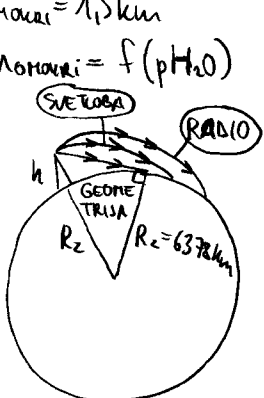
$$\Delta n_0 = 0,0003$$

$$H = 8500 \text{ m}$$

SUHI + MOVKI DEL

$$H_{\text{mokra}} = 1,5 \text{ km}$$

$$\Delta n_{\text{mokra}} = f(p, H_2O)$$



$$n = 1 + \Delta n_{\text{suhi}} e^{-\frac{h}{H_{\text{suhi}}}} + \Delta n_{\text{mokra}} e^{-\frac{h}{H_{\text{mokra}}}}$$

$$R(0) \approx 25000 \text{ km (RADIO)}$$

$$R(0) \approx 50000 \text{ km (SVETLOBA)}$$

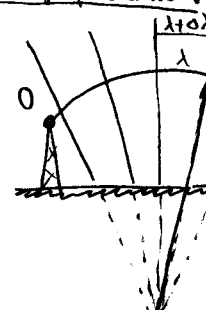
Efektivni polmer Zemlje:

$$\frac{1}{R_{\text{eff}}} = \frac{1}{R_2} - \frac{1}{R}$$

$$R_{\text{eff}} \approx 8600 \text{ km (RADIO)}$$

$$R_{\text{eff}} \approx 7300 \text{ km (SVETLOBA)}$$

Krivljenje žarkov:



$$\lambda = \frac{\lambda_0}{n}$$

$$\lambda = \frac{\lambda_0}{1 + \Delta n_0 e^{-\frac{h}{H}}}$$

$$\frac{d\lambda}{dh} = \frac{-\lambda_0}{h^2} \Delta n_0 \left(-\frac{1}{H}\right) e^{-\frac{h}{H}}$$

Podoben trikotniku

$$\frac{\lambda}{R} = \frac{\lambda + d\lambda}{R + dh} = \frac{d\lambda}{dh} \approx \lambda \frac{d\lambda}{dh} e^{-\frac{h}{H}}$$

$$R = \frac{H}{\Delta n_0} e^{\frac{h}{H}}$$

$$h=0 \rightarrow R(0) = 28333 \text{ km}$$

Zgled: Stolp

$$h = 100 \text{ m}$$

$$d = ?$$

$$(R_2 + h)^2 = R_2^2 + d^2$$

$$R_2^2 + 2R_2 h + h^2 = R_2^2 + d^2$$

$$d = \sqrt{2R_2 h + h^2} \approx \sqrt{2R_2 h}$$

$$\text{Geometrijski doomet: } d = 35,7 \text{ km}$$

$$(R_2 = 6378 \text{ km})$$

$$\text{Svetlobni doomet: } d = 38,2 \text{ km}$$

$$(R_{\text{eff}} = 7300 \text{ km})$$

$$\text{Radijski doomet: } d = 41,5 \text{ km}$$

$$(R_{\text{eff}} = 8600 \text{ km})$$

Lom ob sončnem zahodu:

$$n_1 = 1,00045$$

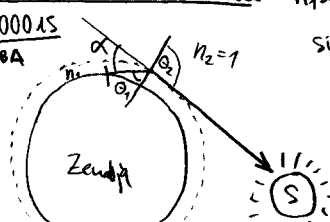
$$\text{SVETLOBA}$$

$$n_2 = 1$$

$$\sin \theta_1 = \frac{n_2}{n_1} = \cos \alpha$$

$$\alpha = \arccos \frac{1}{n_1}$$

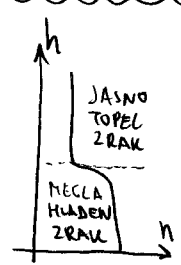
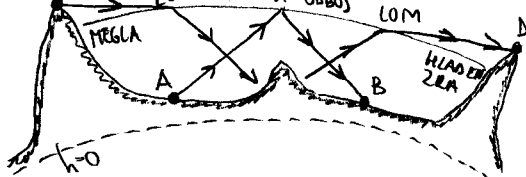
$$\alpha \approx 1^\circ$$



INVERZIJA:

TOPEL ZRAK

JASNO



Ponovitev:

TROPOSFERA < 10 km

$$n = 1 + \Delta n e^{-\frac{h}{H}}$$

$$\Delta n_{\text{skl}} = 0,0003$$

$$H_{\text{skl}} = 8,5 \text{ km}$$

$$H_{\text{mudi}} = 1,5 \text{ km}$$

$$R \approx 25000 \text{ km} @ h=0$$

$$R_{\text{eff}} \approx 4/3 R_z$$

IONOSFERA:

$$h > 60 \text{ km}$$

$$\vec{F} = Q\vec{E} = m\vec{a} = m j \omega \vec{r}$$

$$\vec{r} = \frac{Q}{j \omega m} \vec{E} \quad N [\text{m}^{-3}]$$

$$\vec{j} = N Q \vec{r} = \frac{N Q^2}{j \omega m} \vec{E}$$

KONVEKTIVNI TOK

belci:

$$m_p \approx 1800 m_e$$

$$m_{\text{ion}} > m_p$$

samo elektroni!

$$m_e = 9,1 \cdot 10^{-31} \text{ kg}$$

$$Q_e = -1,6 \cdot 10^{-19} \text{ As}$$

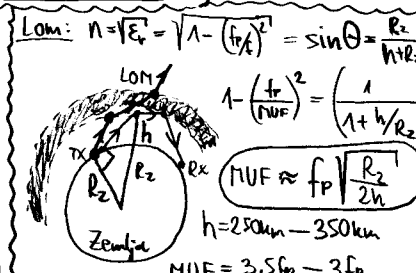
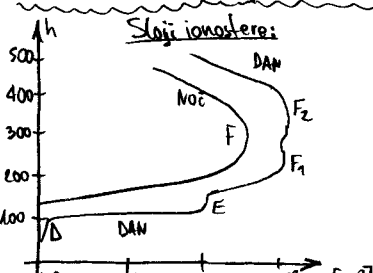
$$\vec{j} = \frac{N Q_e^2}{j \omega m_e} \vec{E}$$

$$\text{rot } \vec{H} = \vec{j} + j \omega \epsilon_0 \vec{E} = \frac{N Q_e^2}{j \omega m_e} \vec{E} + j \omega \epsilon_0 \vec{E}$$

$$\text{rot } \vec{H} = j \omega \epsilon_0 \left(1 - \frac{N Q_e^2}{\omega^2 m_e} \right) \vec{E}$$

$$\epsilon_r = 1 - \frac{N Q_e^2}{\omega^2 \epsilon_0 m_e} = 1 - \frac{f_p^2}{f^2} \quad f_p = \frac{1}{2\pi} \sqrt{\frac{N Q_e^2}{\epsilon_0 m_e}} \approx \begin{cases} 12 \text{ MHz} & \text{DAN} \\ 4 \text{ MHz} & \text{NOČ} \end{cases}$$

Zgled: $f_p = 12 \text{ MHz} \rightarrow N_e = \frac{\epsilon_0 m_e}{Q_e^2} (2\pi f_p)^2 = 1,8 \cdot 10^{12} \text{ elektroni/m}^3$



Slabjenje: MUF, LUF

	MUF	LUF
DAN	36 MHz	3 MHz
NOČ	12 MHz	—

Fazna in skupinska hitrost:

$$v_f = \frac{\omega}{\beta} = \frac{\omega}{k} = \frac{c_0}{n} = \frac{c_0}{\sqrt{1 - (f_p/f)^2}}$$

$$v_g = \frac{d\omega}{dk} = c_0 \sqrt{1 - (f_p/f)^2} < c_0$$

Pogreški GPS @ 1575,42 MHz >> f_p

$$N_g < c_0 < c_f \quad \text{DAN: } |\Delta \vec{r}| \approx 30 \text{ m!}$$

Živomagnetna rezonanca:

Zemljino magnetno polje $H_0 \approx 40 \text{ A/m}$

$$\vec{\omega}_g = \frac{Q \mu_0}{m_e} \vec{H}_0 \quad f_g \approx 1,4 \text{ MHz}$$

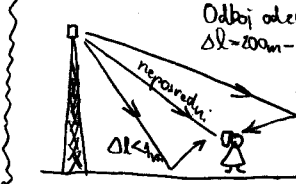
Visoko slabljenje

Faraday-eva suhovala polarizacije

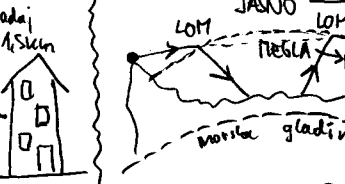
Presih: večpotje v ionosferi:



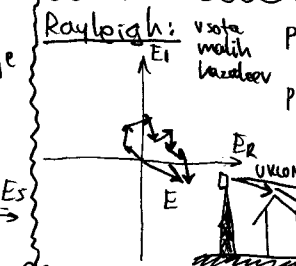
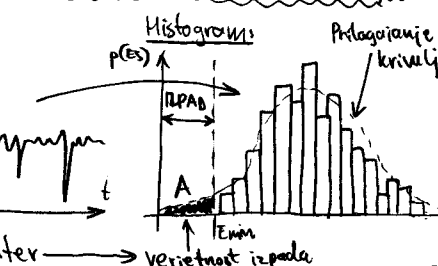
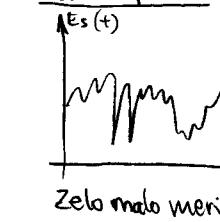
Večpotje mobilni telefoniji:



Presih zaradi inverzije



Meritev presiha:



Rayleigh:

$$p(E_s) = \frac{1}{\sigma^2} e^{-\frac{E_s^2}{2\sigma^2}} \quad E = E_R + jE_I = E_s e^{j\varphi}$$

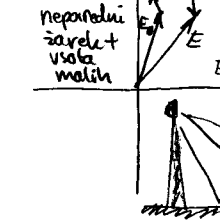
$$p(E_I) = \frac{1}{\sigma^2} e^{-\frac{E_I^2}{2\sigma^2}} \quad p(E_s) = \int_0^{2\pi} p(E_I) p(E_I) E_I d\varphi$$

$$p(E_s) = \frac{E_s}{\sigma^2} e^{-\frac{E_s^2}{2\sigma^2}}$$

$$P_{\text{izpada}} = \int_{E_{\text{min}}}^{\infty} p(E_s) dE_s$$

Samo en podatek

Rice:



Bessel-ova funkcija

$$p(E_s) = \frac{E_s}{\sigma^2} e^{-\frac{E_s^2}{2\sigma^2}} I_0\left(\frac{E_s E_0}{\sigma^2}\right)$$

dva podatka σ in E_0

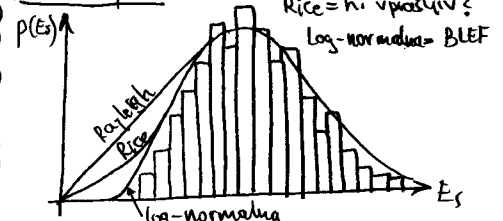
Log-normalna

$$E_{\text{dB}} = 20 \log |E/E_{\text{REF}}|$$

$$p(E_{\text{dB}}) = \frac{1}{\sqrt{2\pi}} e^{-\frac{(E_{\text{dB}} - m_{\text{dB}})^2}{2\sigma_{\text{dB}}^2}}$$

dva podatka m_{dB} in σ_{dB}

Primerjava:



Rayleigh za moč:

$$P_s = \alpha E_s^2 = \alpha (E_R^2 + E_I^2)$$

$$\langle P_s \rangle = \alpha (\langle E_R^2 \rangle + \langle E_I^2 \rangle) = \alpha 2\sigma^2$$

$$P_{\text{izpada}} = \int_{E_{\text{min}}}^{\infty} \frac{E_s}{\sigma^2} e^{-\frac{E_s^2}{2\sigma^2}} dE_s = \int_{E_{\text{min}}^2}^{\infty} \frac{1}{2\sigma^2} e^{-\frac{E_s^2}{2\sigma^2}} dE_s = \int_{\frac{P_{\text{min}}}{\langle P_s \rangle}}^{\infty} \frac{1}{\langle P_s \rangle} e^{-\frac{P_s}{\langle P_s \rangle}} dP_s = 1 - e^{-\frac{P_{\text{min}}}{\langle P_s \rangle}}$$

Zgled: GSM telefon

$$P_{\text{min}} = -105 \text{ dBm} = 31,6 \cdot 10^{-15} \text{ W}$$

$$\langle P_s \rangle = -90 \text{ dBm} = 10^{-12} \text{ W}$$

$$P_{\text{izpada}} = ?$$

$$P_{\text{izpada}} = 1 - e^{-\frac{P_{\text{min}}}{\langle P_s \rangle}} = 1 - e^{-\frac{31,6}{1000}} = 0,0311 = 3,11\%$$

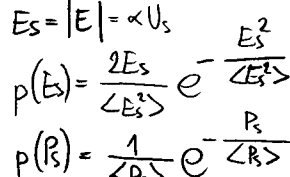
Približek: $P_{\text{min}} \ll \langle P_s \rangle$

$$e^{-x} = 1 - x + \frac{x^2}{2} - \frac{x^3}{6} + \dots \approx 1 - x$$

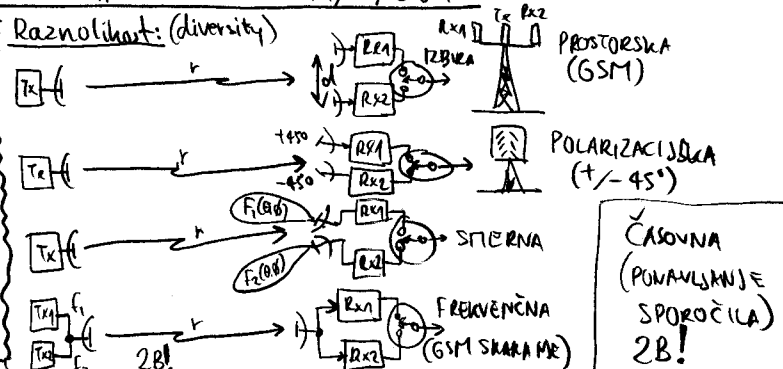
$$P_{\text{izpada}} = 1 - e^{-\frac{P_{\text{min}}}{\langle P_s \rangle}} \approx \frac{P_{\text{min}}}{\langle P_s \rangle} = 3,16\%$$

14/1/2014

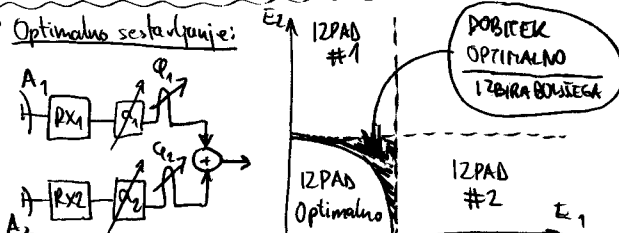
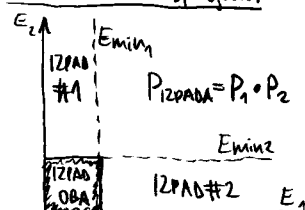
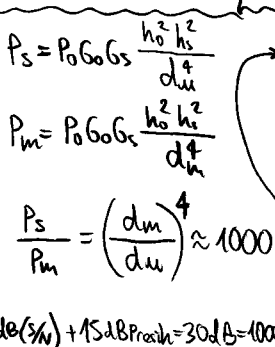
Raznolikost: (diversity)

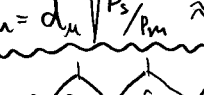


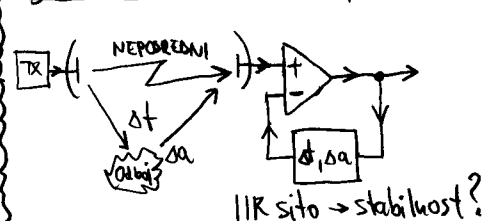
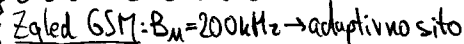
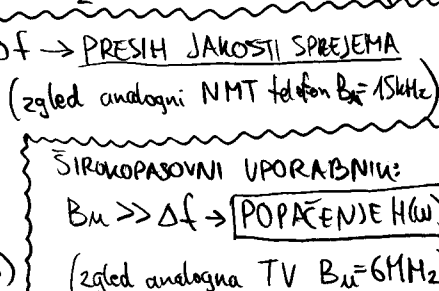
$$P_{127\text{max}} = \int_0^{\text{max}} P(P_s) dP_s = 1 - e^{-\frac{P_{\text{min}}}{\langle P_s \rangle}} = 1 - e^{-\frac{E_{\text{min}}}{\langle E_s \rangle}}$$



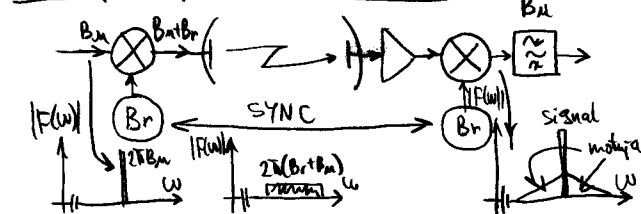
Nekorolitan sprejem:


$$f_1 f_2 \dots f_n \propto h^n$$


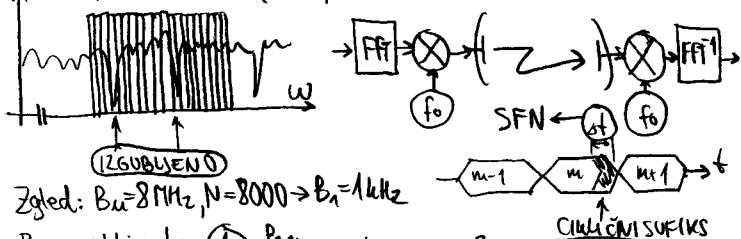
$d_m = d_n \sqrt{\frac{P_s}{P_m}} \approx 5.6 \cdot d_n$ Celice:
 $d_m \approx 5 d_n$

 TLORIS (zeoliteoid)



Razširjeni spekter: $B_r \gg B_m$ UMTS: $B_r = 5 \text{ MHz}$



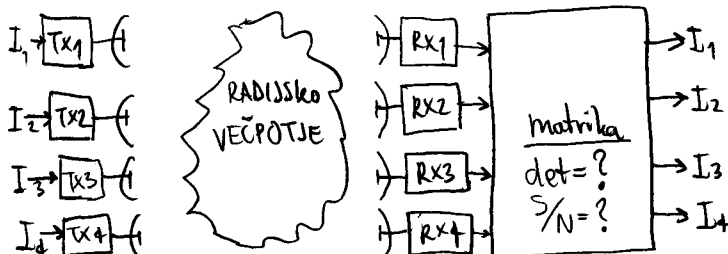
$\Delta H(\omega) \xrightarrow{\text{N ozkopsornih (DVB-T, LTE) uporabnikov na N} \gg \text{1 ozkopsornih}}$



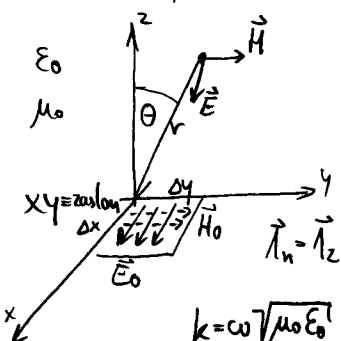
Pomanklijivost: $\textcircled{1} \frac{P_{\max}}{\langle P \rangle} \approx N \rightarrow \eta_{TX} = ?$

② Odstopanje frekvence $< 10\% B_1 \rightarrow$ Doppler?

Zigled 4x4:



MIMO 2x2 = POLARIZACIJSKI MUX
(WiFi, LTE)



$$\begin{aligned} \vec{E}_0 &= \vec{I}_x E_0 \\ \vec{H}_0 &= \vec{I}_y \frac{E_0}{Z_0} \\ \vec{K} &= \vec{I}_n \times \vec{H}_0 = -\vec{I}_x \frac{E_0}{Z_0} \\ \vec{K}_m &= \vec{E}_0 \times \vec{I}_n = -\vec{I}_y E_0 \end{aligned}$$

$$\vec{E}_1 = \vec{I}_{\theta x} \frac{jkZ_0}{4\pi} I_{\Delta x} \frac{e^{-jkr}}{r} \sin \theta_x = -\vec{I}_{\theta x} \frac{jkZ_0}{4\pi} |\vec{K}| \Delta y \Delta x \frac{e^{-jkr}}{r} \sin \theta_x$$

$$\vec{E}_1 = -\vec{I}_{\theta x} \frac{jk}{4\pi} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} \sin \theta_x$$

$$\vec{E}_2 = -\vec{I}_{\phi y} \frac{jk}{4\pi} I_{\Delta y} \frac{e^{-jkr}}{r} \sin \theta_y = \vec{I}_{\phi y} \frac{jk}{4\pi} |\vec{K}_m| \Delta x \Delta y \frac{e^{-jkr}}{r} \sin \theta_y$$

$$\vec{E}_2 = \vec{I}_{\phi y} \frac{jk}{4\pi} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} \sin \theta_y$$

$$\vec{E} = \vec{E}_1 + \vec{E}_2 = \frac{jk}{4\pi} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} [-\vec{I}_{\theta x} \sin \theta_x + \vec{I}_{\phi y} \sin \theta_y]$$

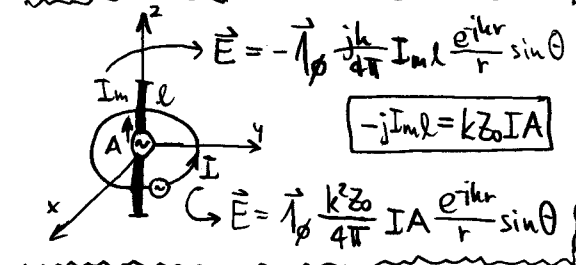
$$-\vec{I}_{\theta x} \sin \theta_x + \vec{I}_{\phi y} \sin \theta_y = (\cos \theta + 1) [\vec{I}_{\theta} \cos \phi - \vec{I}_{\phi} \sin \phi]$$

$$\vec{E} = (\vec{I}_{\theta} \cos \phi - \vec{I}_{\phi} \sin \phi) \frac{jk}{4\pi} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} (\cos \theta + 1)$$

$$\vec{E} = (\vec{I}_{\theta} \cos \phi - \vec{I}_{\phi} \sin \phi) \frac{j}{2\lambda} E_0 \Delta x \Delta y \frac{e^{-jkr}}{r} (\cos \theta + 1)$$

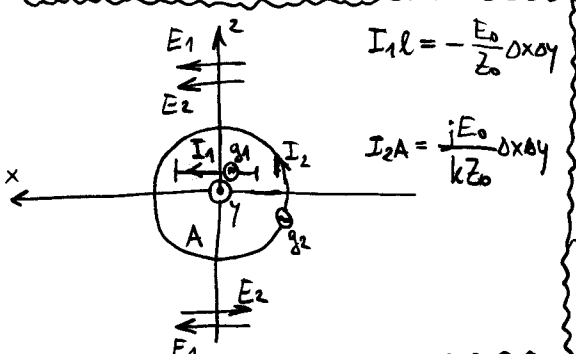
endni vektor!
POLARRACISA

$F(\theta, \phi)$



$$-jI_{ml} = kZ_0 IA$$

$$\vec{E} = \vec{I}_{\phi} \frac{k^2 Z_0}{4\pi} IA \frac{e^{-jkr}}{r} \sin \theta$$



$$I_1 l = -\frac{E_0}{Z_0} \Delta x \Delta y$$

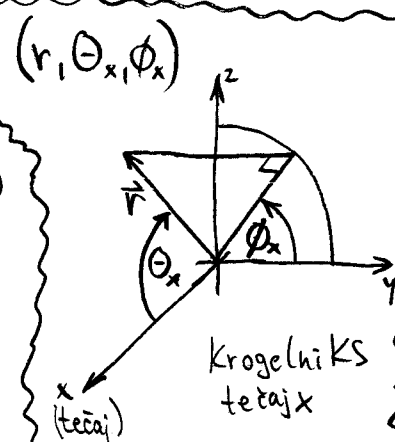
$$I_2 A = \frac{jE_0}{kZ_0} \Delta x \Delta y$$

$$\vec{I}_{\theta} = \vec{I}_x \cos \theta \cos \phi + \vec{I}_y \cos \theta \sin \phi - \vec{I}_z \sin \theta$$

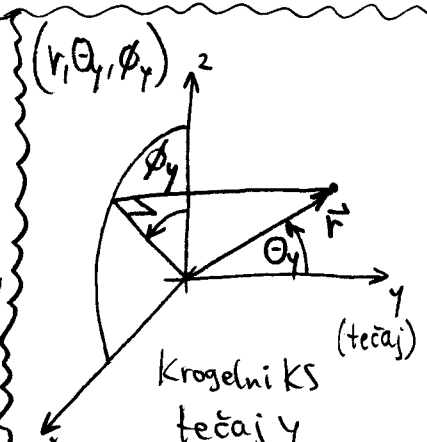
$$\vec{I}_{\phi} = -\vec{I}_x \sin \phi + \vec{I}_y \cos \phi$$

$$\cos \theta = \frac{z}{r} \quad \sin \theta = \frac{\sqrt{x^2 + y^2}}{r}$$

$$\cos \phi = \frac{x}{\sqrt{x^2 + y^2}} \quad \sin \phi = \frac{y}{\sqrt{x^2 + y^2}}$$



Krogelni KS
tečaj x



Krogelni KS
tečaj y

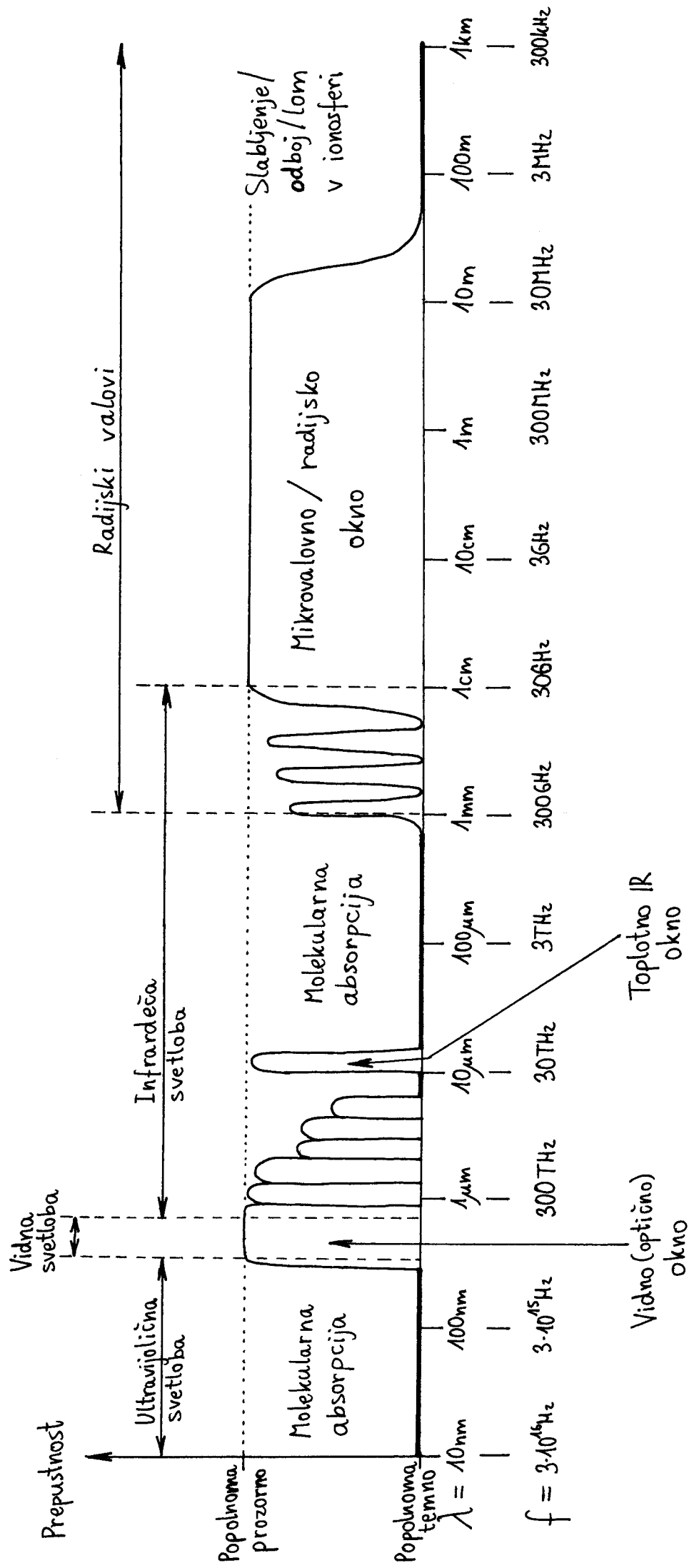
$$\vec{I}_{\theta_x} = \vec{I}_y \cos \theta_x \cos \phi_x + \vec{I}_z \cos \theta_x \sin \phi_x - \vec{I}_x \sin \theta_x = \vec{I}_y \frac{xy}{r\sqrt{y^2+z^2}} + \vec{I}_z \frac{xz}{r\sqrt{y^2+z^2}} - \vec{I}_x \frac{\sqrt{y^2+z^2}}{r} \sin \theta_x = \frac{\sqrt{y^2+z^2}}{r}$$

$$-\vec{I}_{\theta_x} \sin \theta_x = -\vec{I}_y \frac{xy}{r^2} - \vec{I}_z \frac{xz}{r^2} + \vec{I}_x \frac{y^2+z^2}{r^2} = \vec{I}_x (1 - \sin^2 \theta \cos^2 \phi) - \vec{I}_y \sin^2 \theta \cos \phi \sin \phi - \vec{I}_z \sin^2 \theta \cos \theta \cos \phi$$

$$\vec{I}_{\phi_y} = -\vec{I}_z \sin \phi_y + \vec{I}_x \cos \phi_y = -\vec{I}_z \frac{x}{\sqrt{z^2+x^2}} + \vec{I}_x \frac{z}{\sqrt{z^2+x^2}} \quad \sin \theta_y = \frac{\sqrt{z^2+x^2}}{r}$$

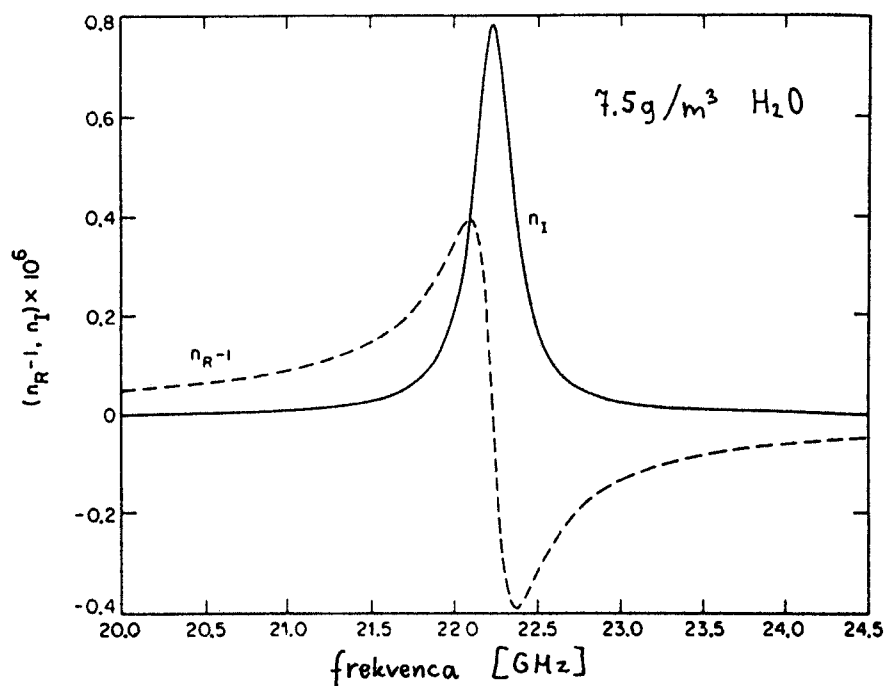
$$\vec{I}_{\phi_y} \sin \theta_y = -\vec{I}_z \frac{x}{r} + \vec{I}_x \frac{z}{r} = \vec{I}_x \cos \theta - \vec{I}_z \sin \theta \cos \phi$$

$$\begin{aligned} -\vec{I}_{\theta_x} \sin \theta_x + \vec{I}_{\phi_y} \sin \theta_y &= \vec{I}_x (1 + \cos \theta - \sin^2 \theta \cos^2 \phi) - \vec{I}_y \sin^2 \theta \cos \phi \sin \phi - \vec{I}_z (1 + \cos \theta) \sin \theta \cos \phi = \\ &= \vec{I}_x (1 + \cos \theta + (\cos^2 \theta - 1) \cos^2 \phi) + \vec{I}_y (\cos^2 \theta - 1) \cos \phi \sin \phi - \vec{I}_z (1 + \cos \theta) \sin \theta \cos \phi = \\ &= (\cos \theta + 1) [\vec{I}_x (1 + \cos \theta \cos^2 \phi - \cos^2 \phi) + \vec{I}_y (\cos \theta \cos \phi \sin \phi - \cos \phi \sin \phi) - \vec{I}_z \sin \theta \cos \phi] = \\ &= (\cos \theta + 1) [\vec{I}_x (\cos \theta \cos^2 \phi + \sin^2 \phi) + \vec{I}_y (\cos \theta \cos \phi \sin \phi - \cos \phi \sin \phi) - \vec{I}_z \sin \theta \cos \phi] = \\ &= (\cos \theta + 1) [\vec{I}_{\theta} \cos \phi - \vec{I}_{\phi} \sin \phi] \end{aligned}$$



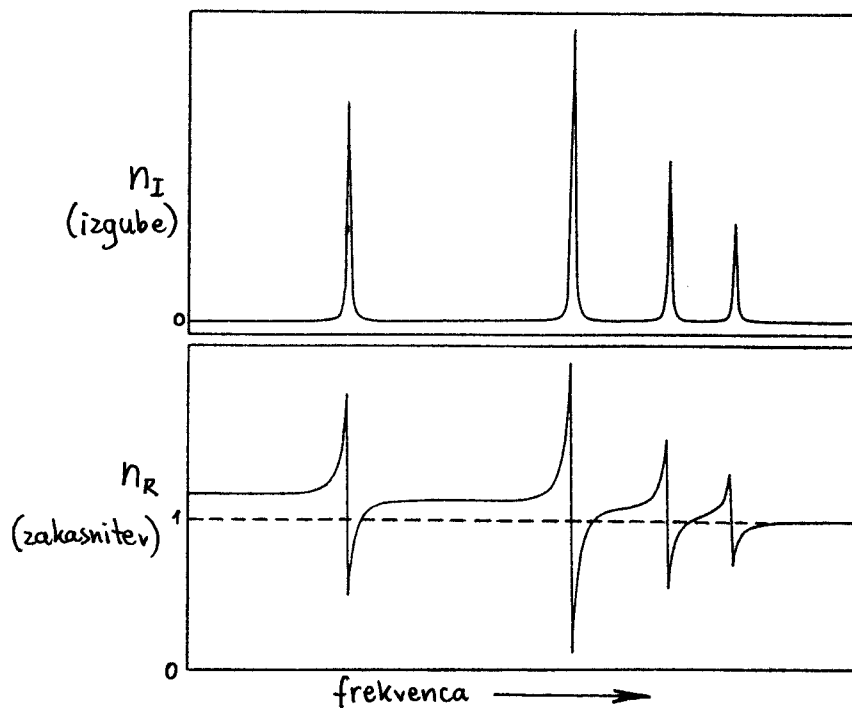
Prepustnost zemeljskega ozračja za elektromagnetno valovanje

Kompleksni
lomni
količnik
 $n = n_R + jn_I$

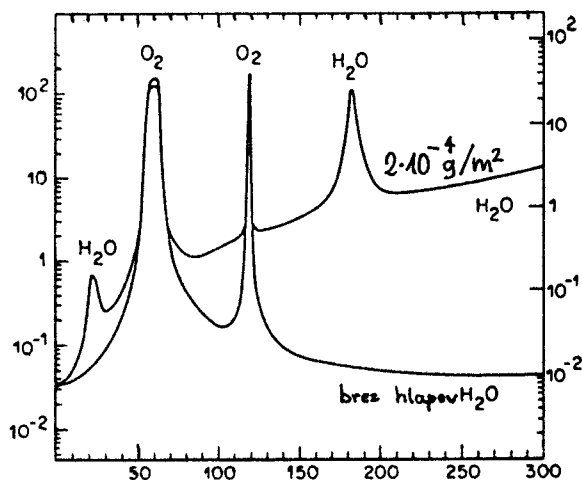


Kompleksni
lomni
količnik

$$n = n_R + jn_I$$



Zenitno
slabljenje
[dB]



Zenitno
slabljenje
[N_p]

Mikrovalovna molekularna absorpcija v zemeljskem ozračju

$$\lambda = \frac{\lambda_0}{n}$$

Lomni količnik v troposferi:

$$n = 1 + \Delta n e^{-\frac{h}{h_0}}$$

R poiščemo iz podobnih trikotnikov:

$$\lambda = \alpha R \quad \alpha \equiv \text{konstanta}$$

$$\frac{d\lambda}{dh} = \alpha \frac{dR}{dh} = \alpha$$

$$\frac{d\lambda}{dh} = \frac{d}{dh} \left(\frac{\lambda_0}{n} \right) = \frac{\lambda_0 \Delta n}{h_0 n^2} e^{-\frac{h}{h_0}}$$

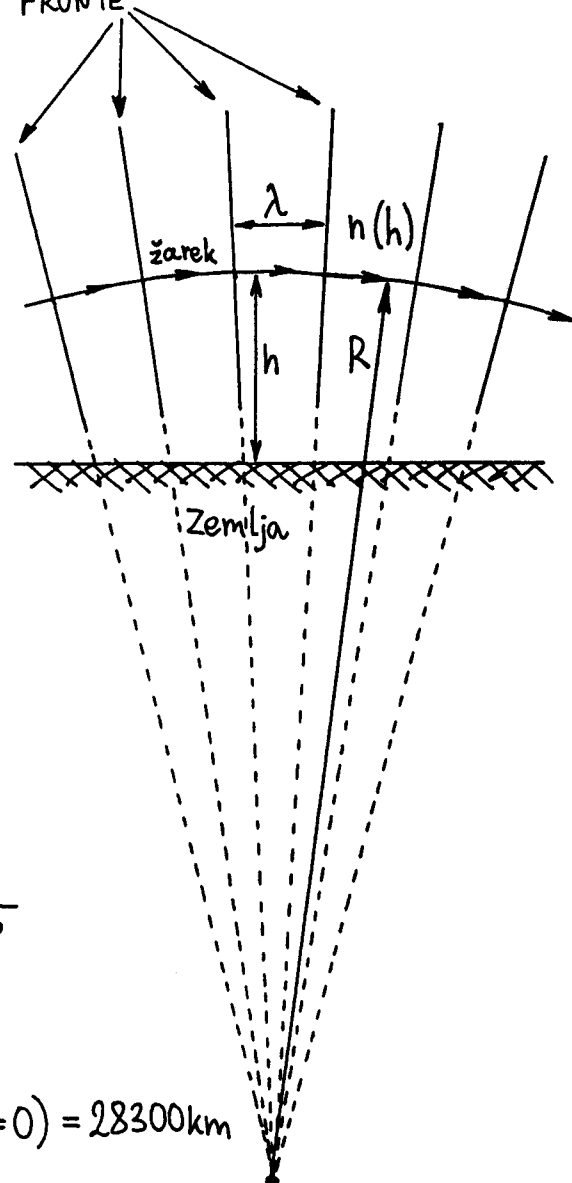
$$R = \frac{\lambda}{\alpha} = \frac{h_0 n^2}{\Delta n} e^{-\frac{h}{h_0}} \approx \frac{h_0}{\Delta n} e^{-\frac{h}{h_0}}$$

Suha troposfera:

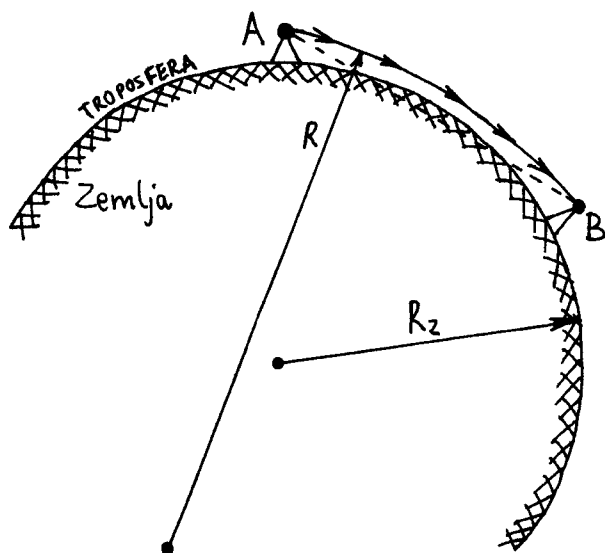
$$h_0 = 8.5 \text{ km} ; \Delta n = 0.0003 \longrightarrow R(h=0) = 28300 \text{ km}$$

$$\text{Vlažna troposfera: } R(h=0) \approx 25000 \text{ km}$$

VALOVNE FRONTE



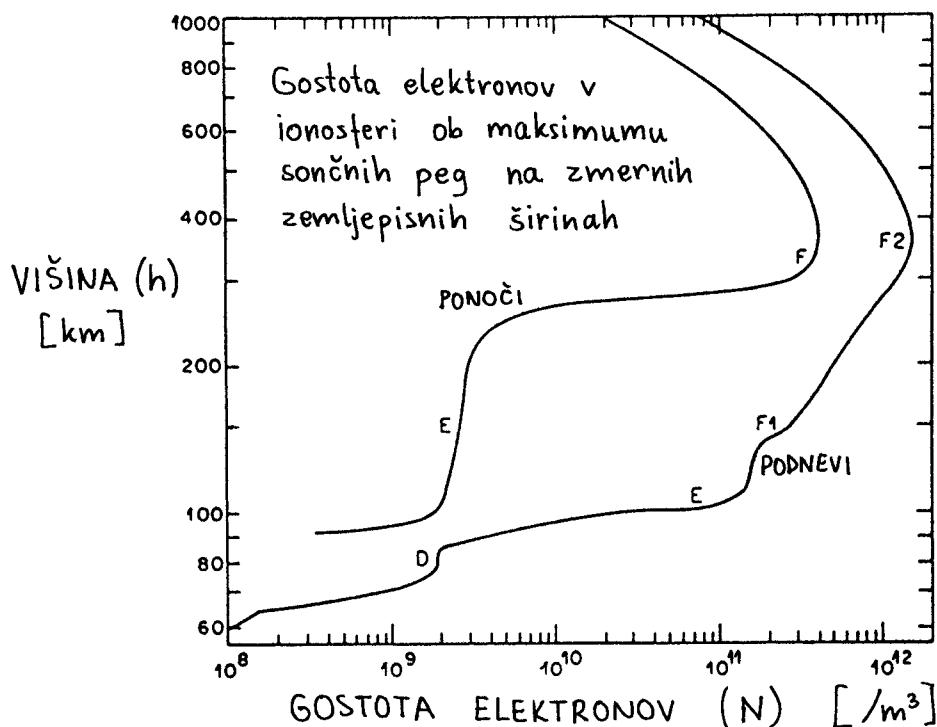
Lom radijskih valov v troposferi



$$\frac{1}{R_e} = \frac{1}{R_z} - \frac{1}{R}$$

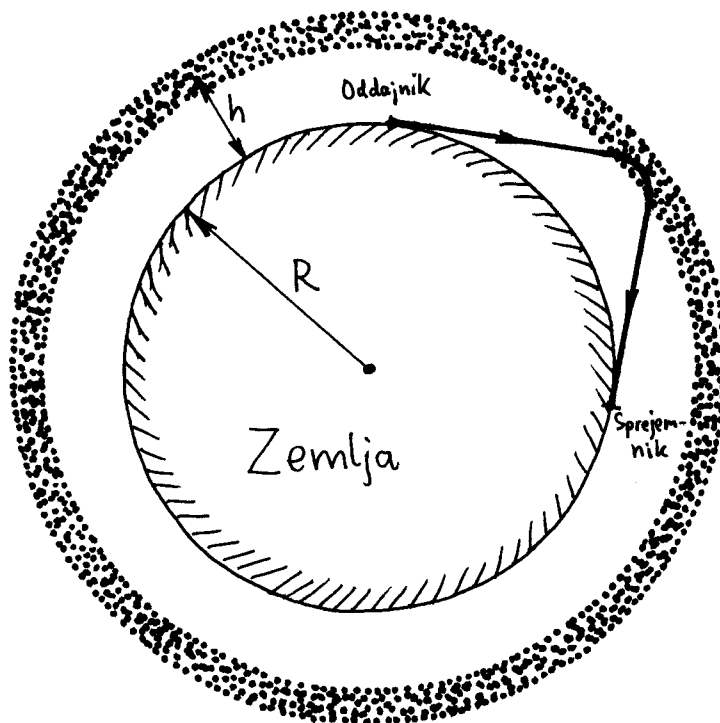
$$R_e \approx 8600 \text{ km} \approx \frac{4}{3} R_z$$

Efektivni polmer zemeljske površine



Lomni količnik: $n = \sqrt{1 - \left(\frac{f_p}{f}\right)^2}$

Frekvenca plazme: $f_p = \frac{1}{2\pi} \sqrt{\frac{NQ_e^2}{\epsilon_0 m_e}} = \sqrt{80.8 \frac{\text{m}^3}{\text{s}^2} N} = \begin{cases} \text{max} \\ \sim 12 \text{ MHz} \\ \text{PODNEVI} \\ \text{-----} \\ \text{max} \\ \sim 4 \text{ MHz} \\ \text{PONOČI} \end{cases}$



Zaradi loma ob poševnem vpadu valovanja:

$$\text{MUF} > f_p$$

$$\text{MUF} \approx f_p \sqrt{\frac{R}{2h}}$$

$$\text{MUF} \approx 3 f_p$$

$$\text{MUF} \approx \begin{cases} 36 \text{ MHz} \text{ PODNEVI} \\ \text{-----} \\ 12 \text{ MHz} \text{ PONOČI} \end{cases}$$

Zelo visoka disperzija (snovna, rodovna) \rightarrow zmogljivost $\sim 100 \text{ bit/s}$

Radijska zveza preko loma/odboja v ionosferi